



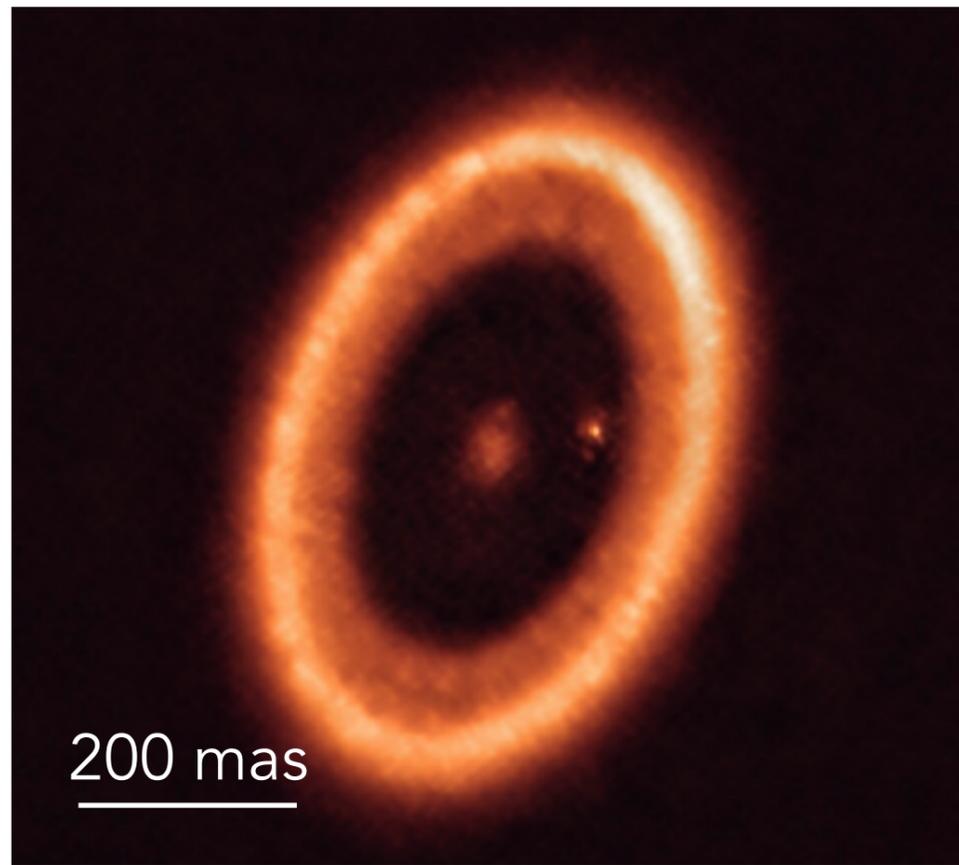
# Observing planet forming disks with ALMA

## Basics of interferometry

Stefano Facchini

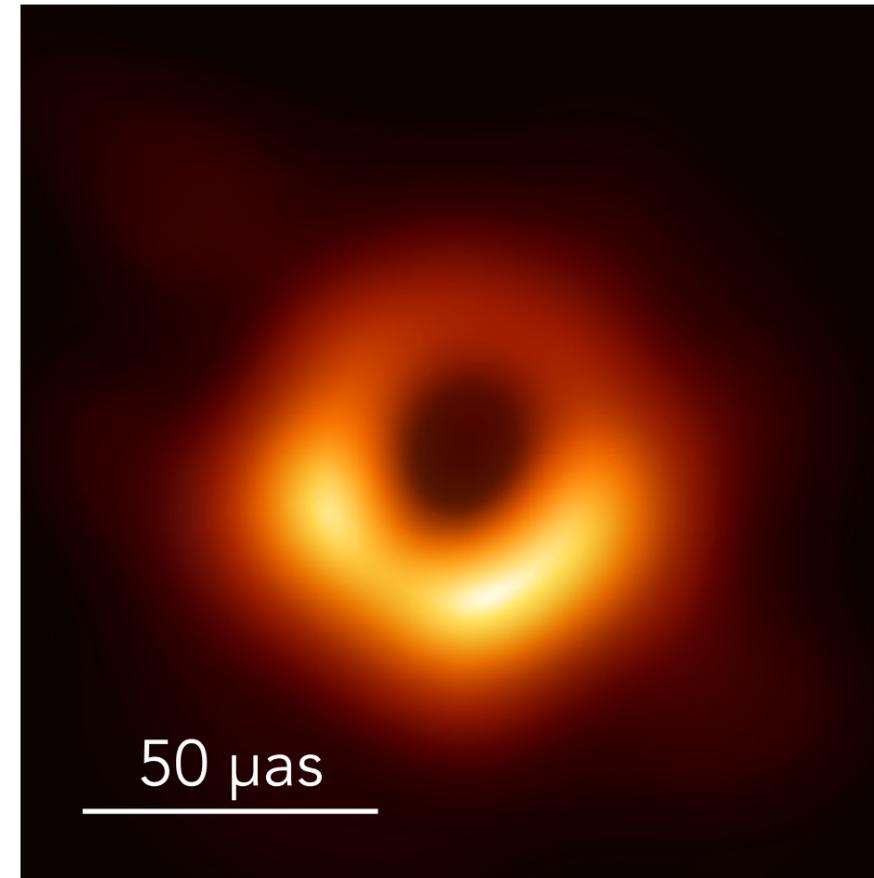


# Need for high angular resolution



*Planetary system  
in formation (Benisty+2021)*

1 au at 100 pc is 10mas



*Torus orbiting a SMBH in M87  
(EHT Collaboration+2021)*

The radius of the shadow of a  
Schwarzschild BH at 16.8 Mpc is 38 μas

Several fundamental physical processes occur on angular scales that are  $<1''$

$$\Theta(\text{arcsec}) = 2\lambda_{\text{cm}}/D_{\text{km}} \longrightarrow \text{antenna of 4 km to have } 0.1'' \text{ a } 2 \text{ mm}$$

Interferometry is necessary to achieve such angular scales.

# Aperture synthesis interferometry - background

For an interferometer formed by two antennas, it is possible to demonstrate that:

$$\Theta(\text{arcsec}) = 2\lambda_{\text{cm}} / B_{\text{km}}$$

where  $B$  is the baseline, i.e. the projected distance of the two antennas



## One-Mile Telescope

- Close to Cambridge, UK
- Opened in 1964
- 3 antennas of 18-m
- First aperture synthesis exploiting the Earth rotation

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## ALMA

- Altiplan of Chajnantor
- First light in 2011
- 54 12-m, 12 7-m antennas

# Going beyond a two element interferometer

A two element interferometer measures the Fourier transform of the sky brightness  $B$ ,  
where  $(u,v)$  are the coordinates of the baseline, and  
 $\hat{A}$  is the primary beam correction

$$V(u, v) = Ae^{-i\phi} = \int \hat{A}(x, y) B(x, y) e^{-i2\pi(ux+vy)} dx dy$$

$A$  is the amplitude, and  $\phi$  is the phase of the complex visibility.

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- $(u,v)$  are the spatial frequencies in the directions E-W e N-S, and represent the projected baseline in units of wavelength  $\lambda$
- $(x,y)$  are the relative distance from a reference point in the direction E-W e N-S
- $(x=0,y=0)$  are known as "phase center"
- The phase  $\phi$  contains information on the position of the structures with spatial frequencies  $(u,v)$  with respect to the phase center
- This FT relation is the van Cittert-Zernike theorem, on which aperture synthesis interferometry is based.

# Going beyond a two element interferometer

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This means that if we have a measure of  $V(u,v)$ ,  
we could reconstruct the sky brightness with a Fourier transform

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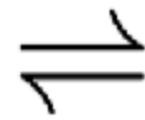
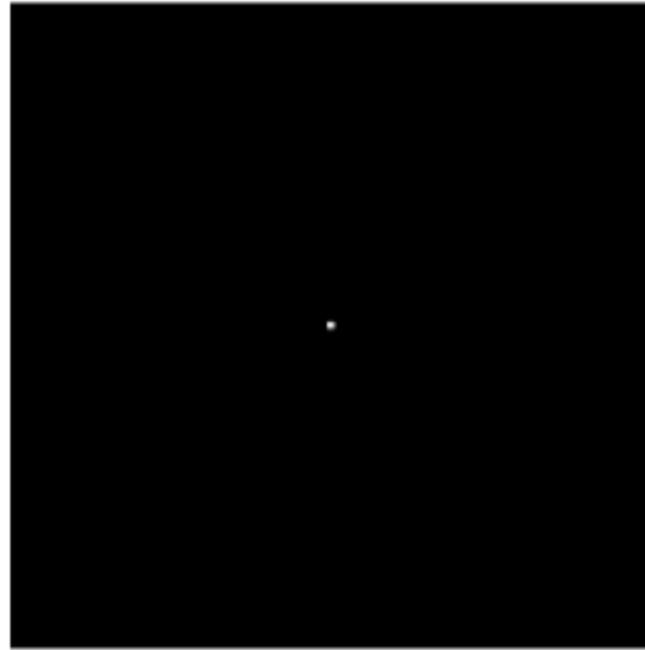
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# Information contained in amplitude and phase

$$I(x, y)$$

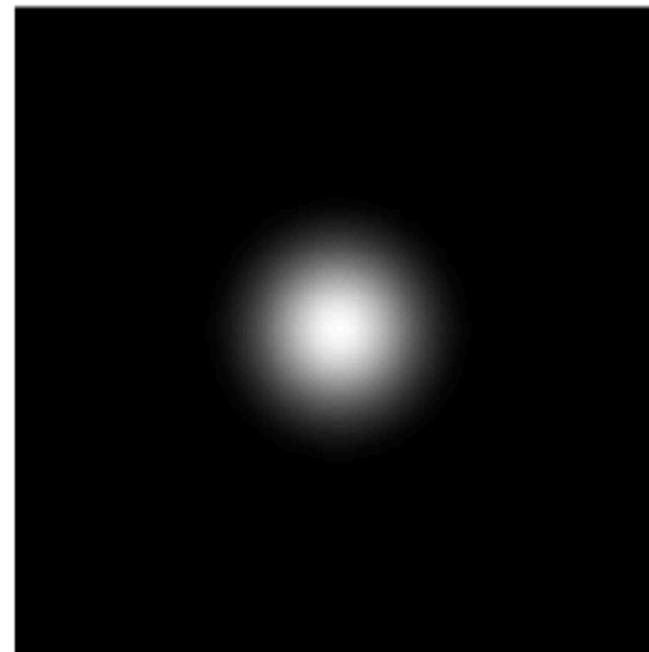
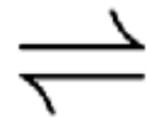
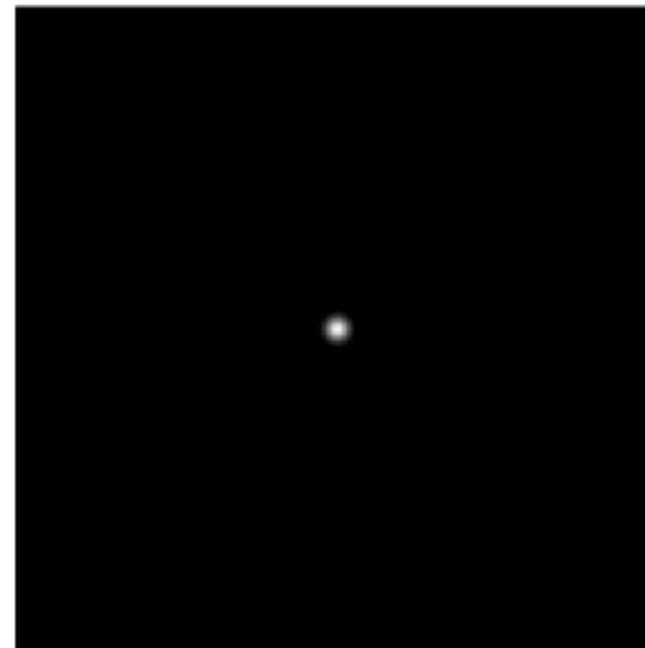
$$A[V(u, v)]$$

$\delta$  Dirac



Constant

Gaussian



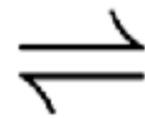
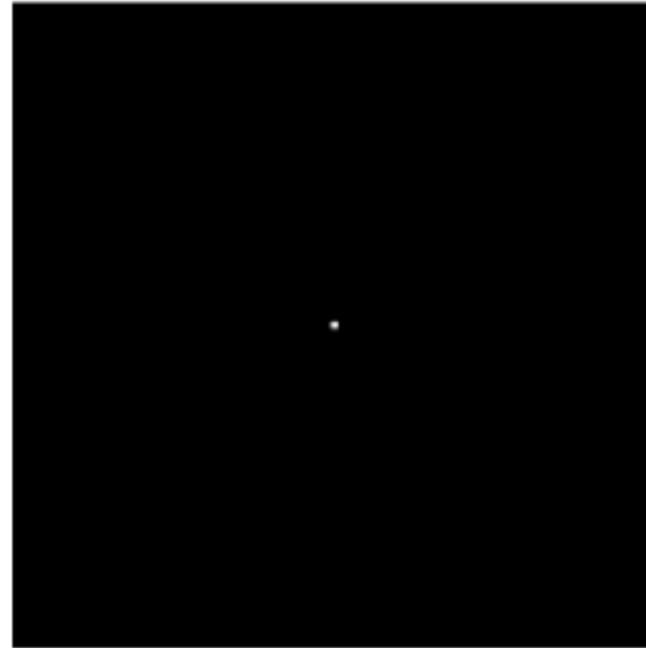
Gaussian

# Information contained in amplitude and phase

$$I(x, y)$$

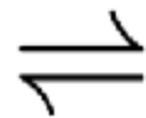
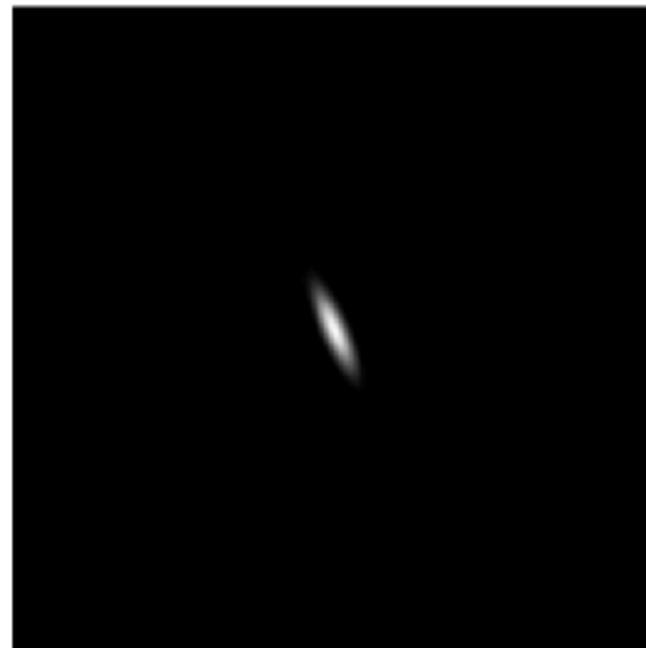
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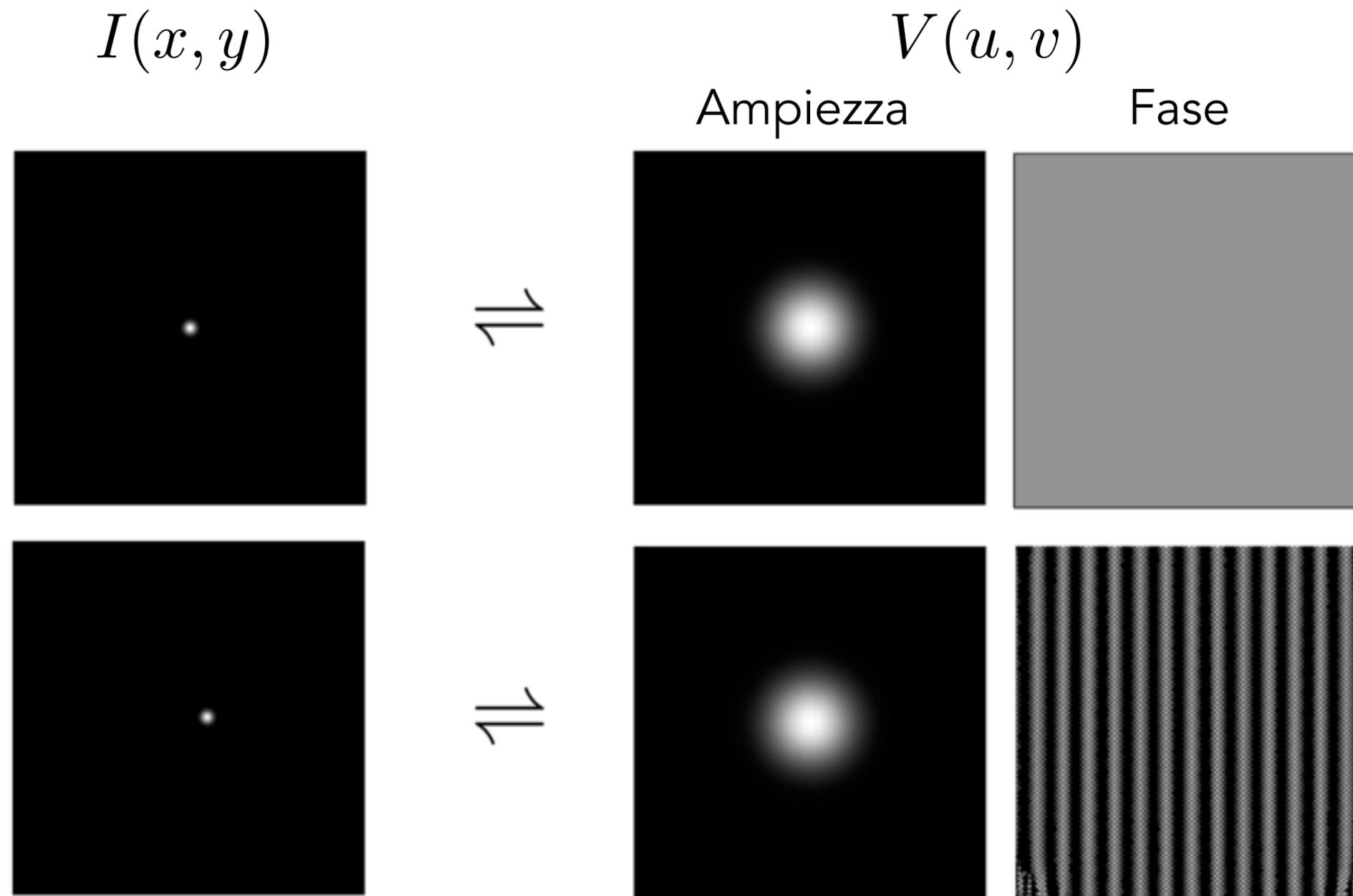
Gaussian



Gaussian

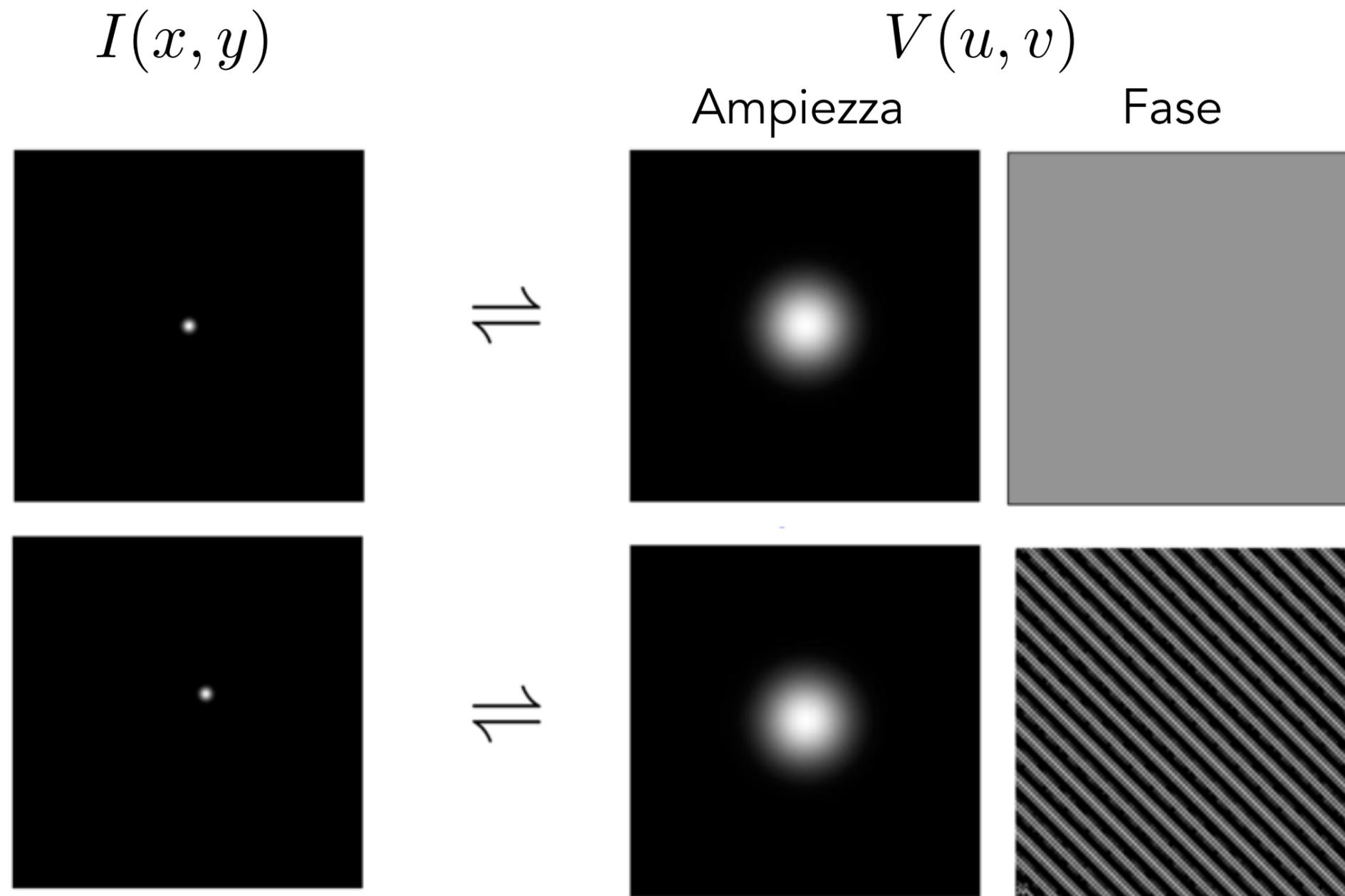
# Information contained in amplitude and phase

The amplitude holds the information on the contribution of different spatial scales, the phase indicates where these spatial scales contribute to



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# Questions we will try to answer in this (1?) h

How to obtain a  $V(u,v)$  as dense as possible?

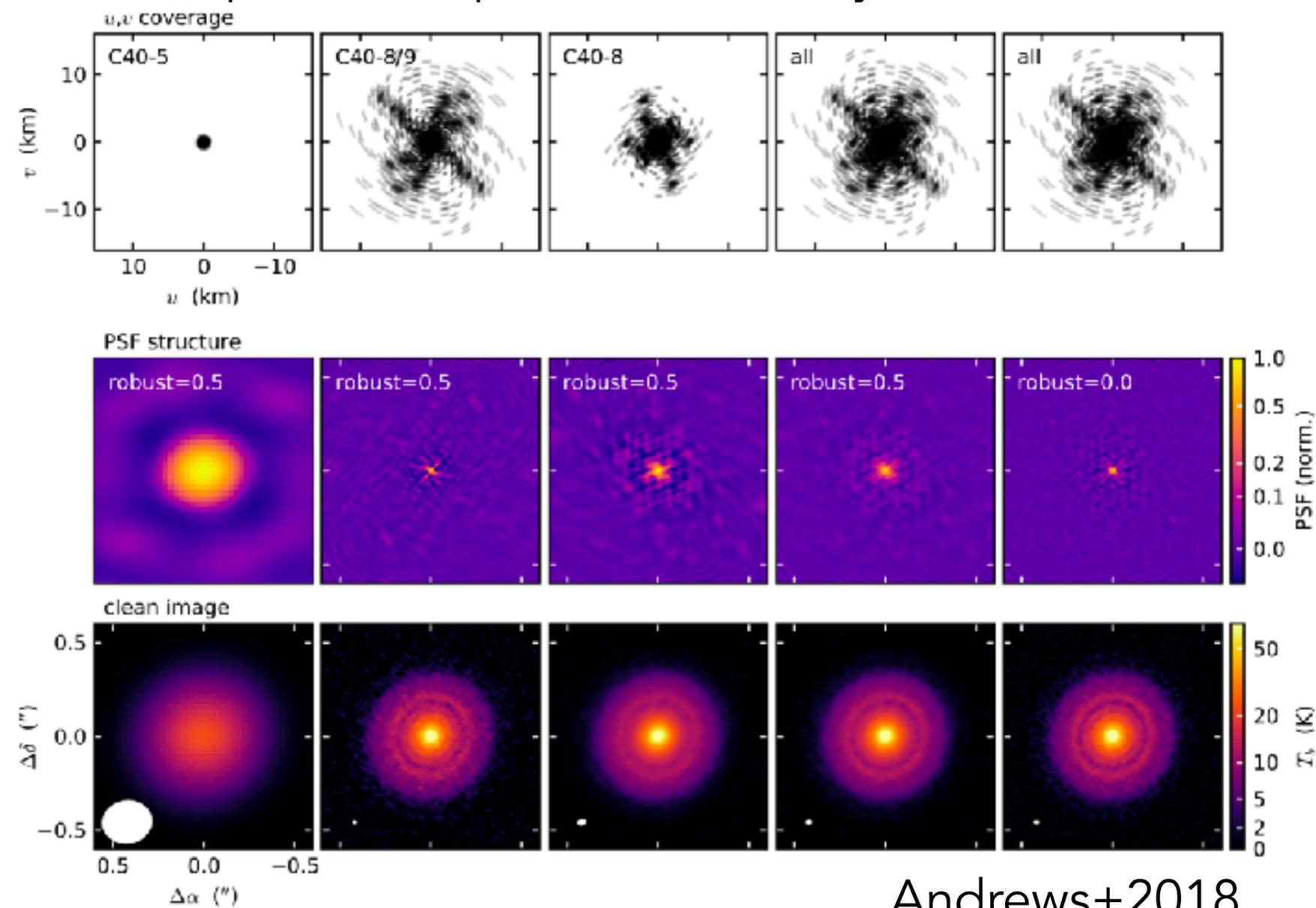
How to calibrate interferometric data (visibilities)?

How to reconstruct an image by having  $V(u,v)$  measured in a discrete set of points?

# How to maximize the sampling of $V(u,v)$ ?

Increase the number of antennas (number of visibilities is  $N(N-1)/2$ ), where  $N$  is the number of antennas. The ALMA 12-m array has 50, ngVLA will have 244.

Use more configurations by moving antennas to physical pads to sample the uv-plane on as many scales as we can



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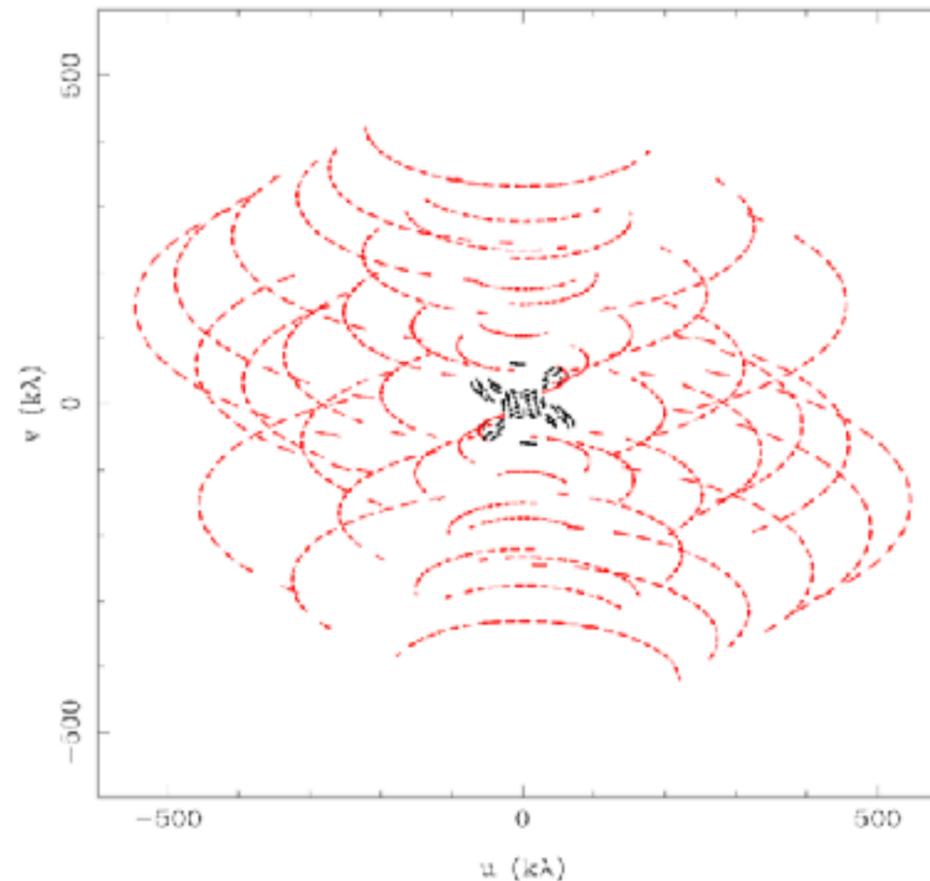
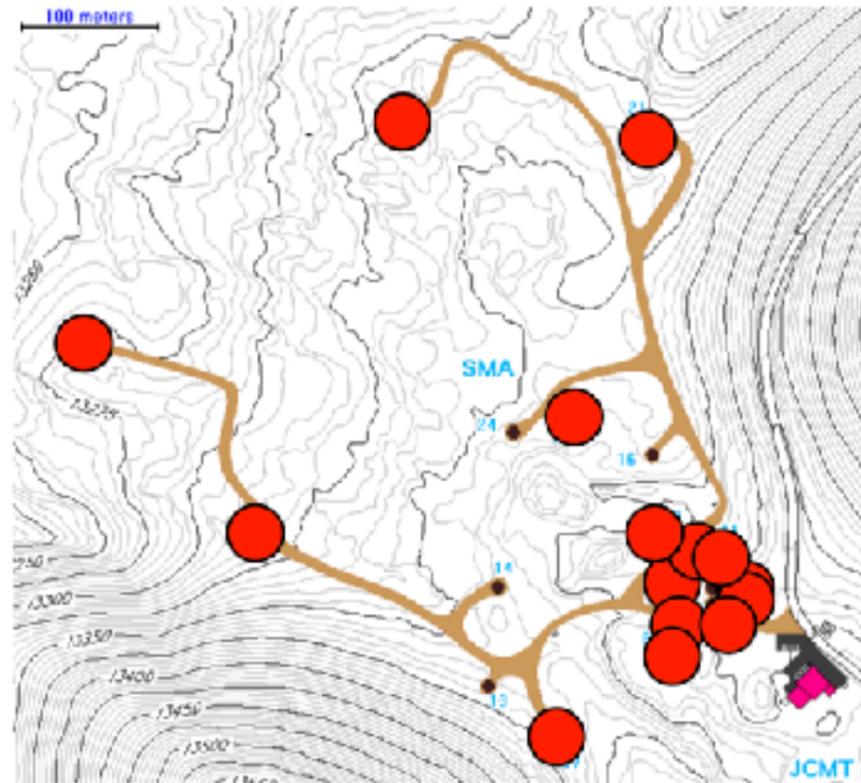
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# How to maximize the sampling of $V(u,v)$ ?

Increase the number of antennas

Exploit the Earth rotation to sample different baselines  
(Martin Ryle, Nobel prize in Physics in 1974)



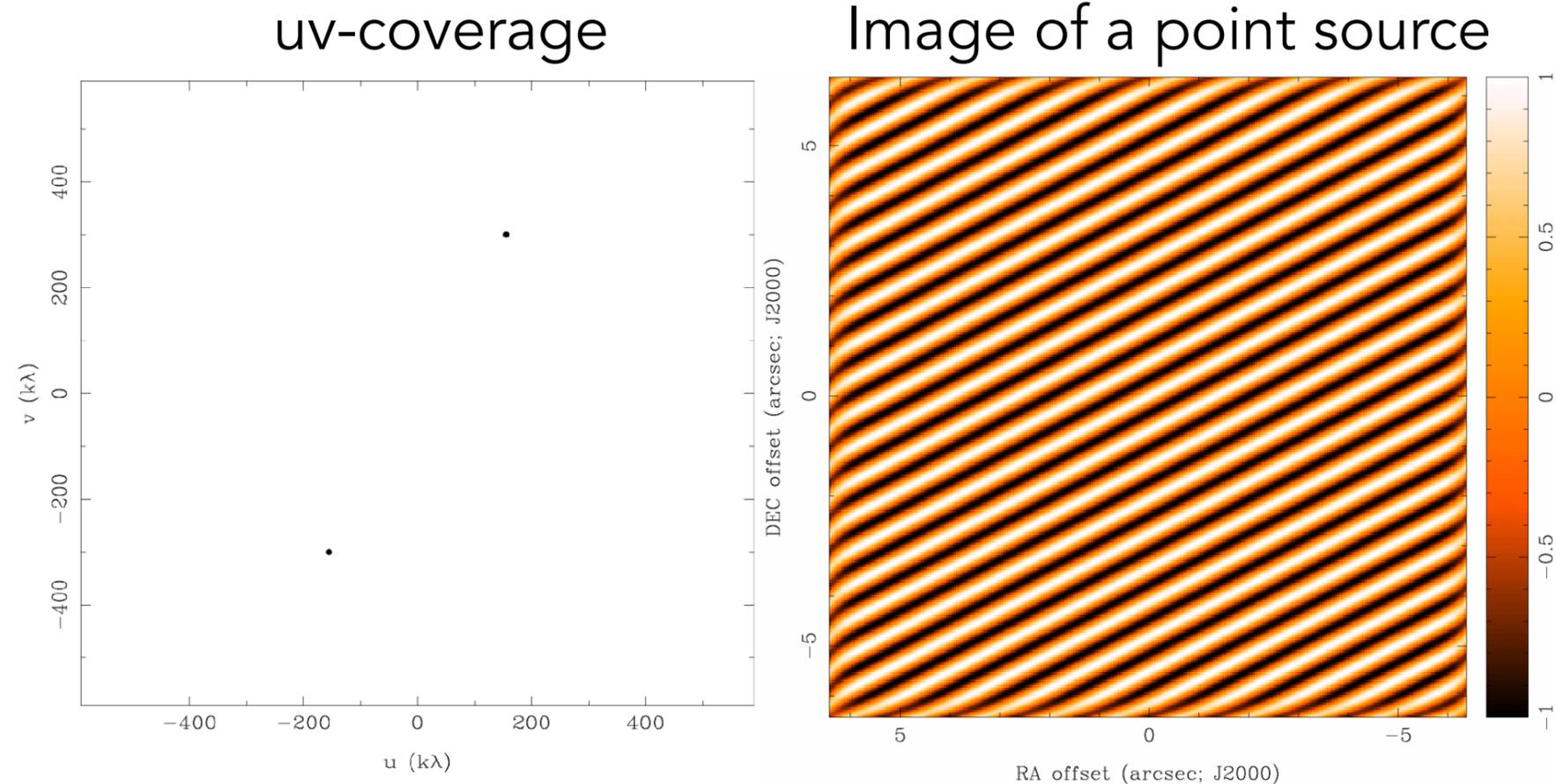
Examples of uv-tracks on SMA with 8 antennas at 345 GHz, Dec = -24 deg

# How to maximize the sampling of $V(u,v)$ ?

Increase the number of antennas

Exploit the Earth rotation to sample different baselines

**2 antennae**

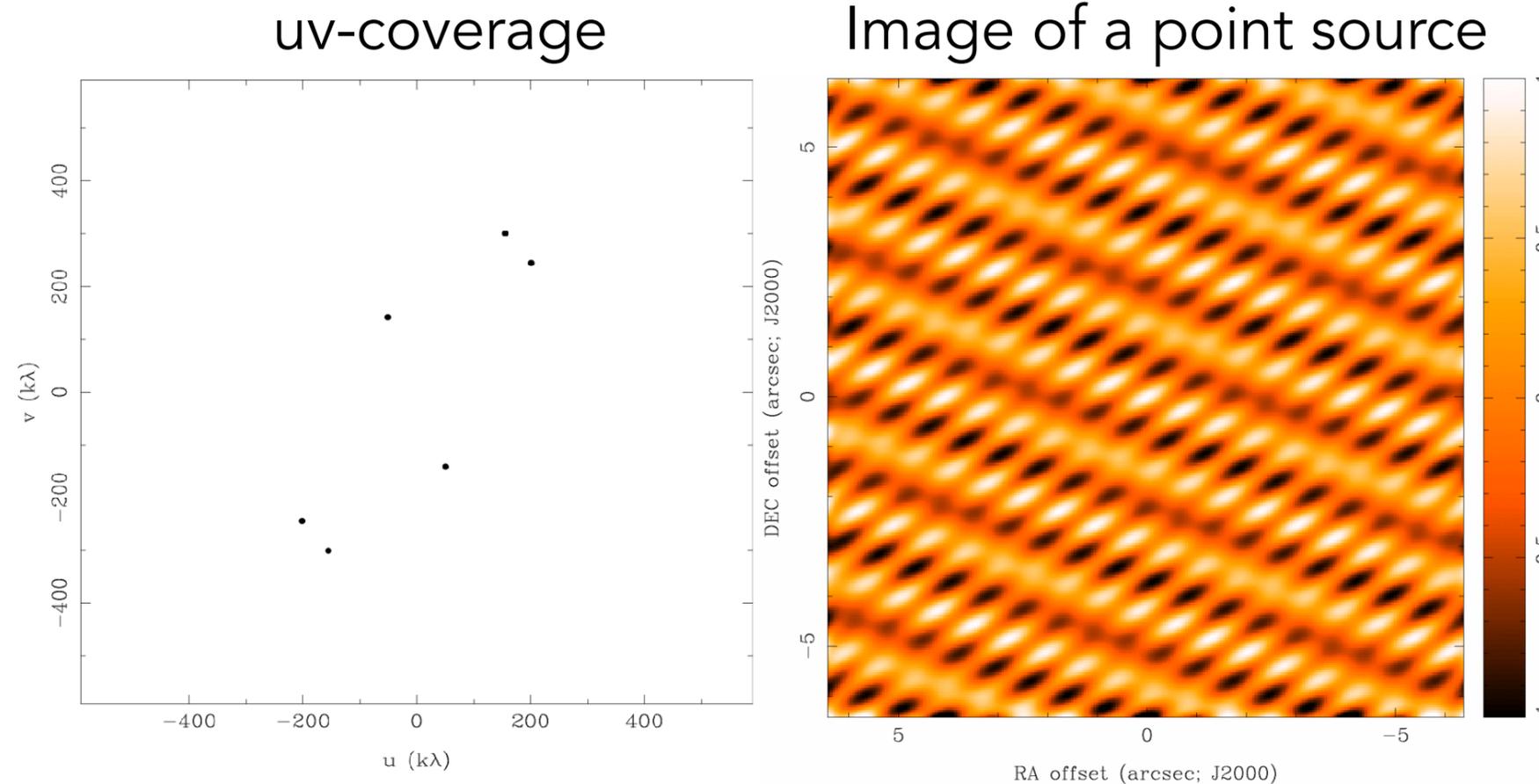


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Increase the number of antennas

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**3 antennae**

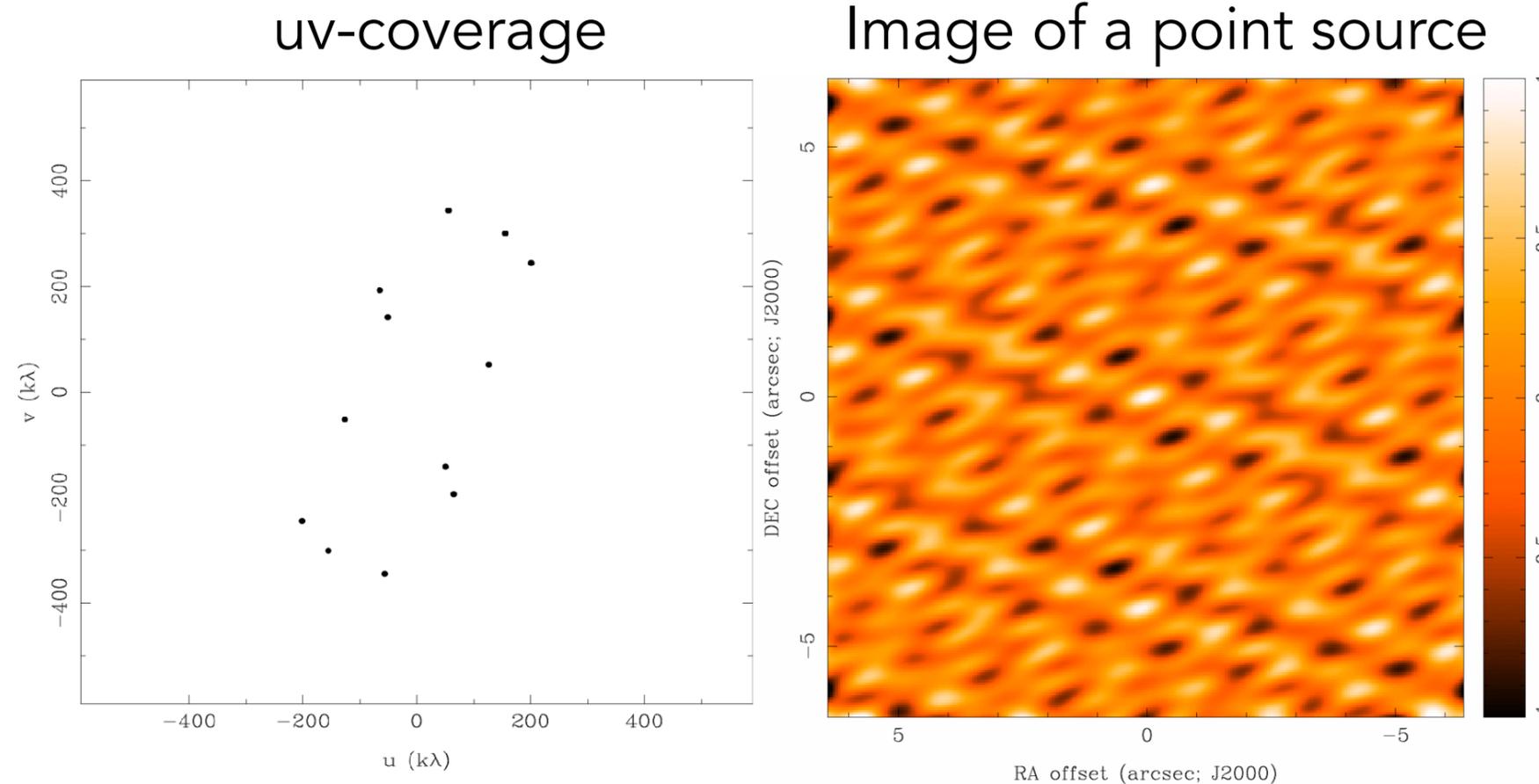


# How to maximize the sampling of $V(u,v)$ ?

Increase the number of antennas

Exploit the Earth rotation to sample different baselines

**4 antennae**



# How to maximize the sampling of $V(u,v)$ ?

Increase the number of antennas

Exploit the Earth rotation to sample different baselines

**5 antennae**

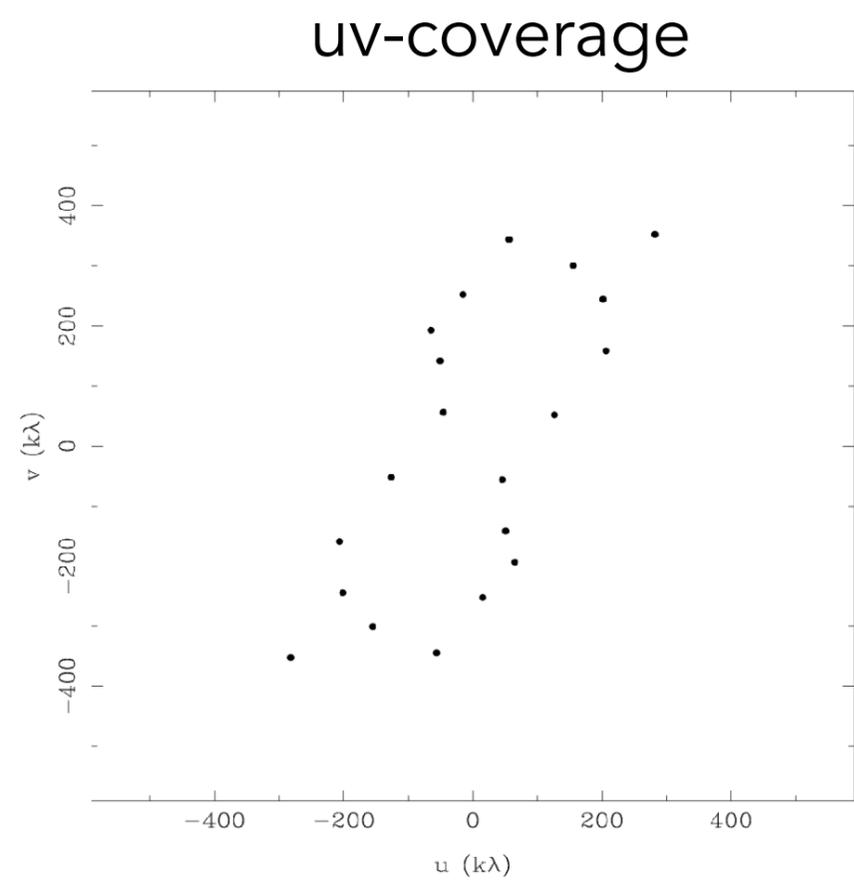
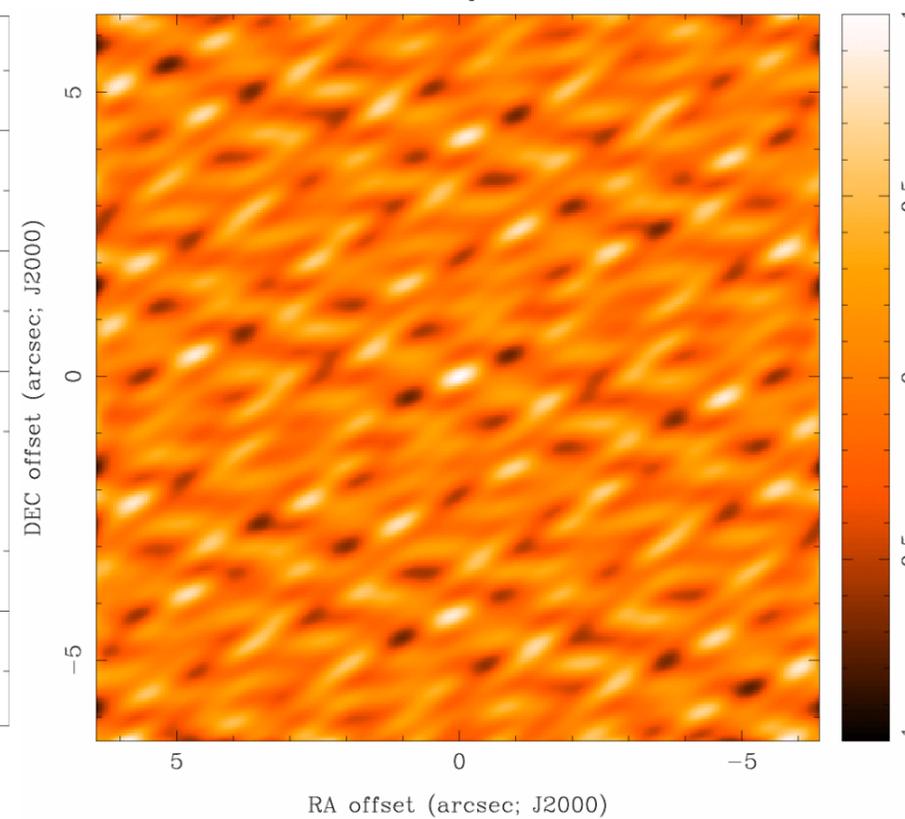


Image of a point source

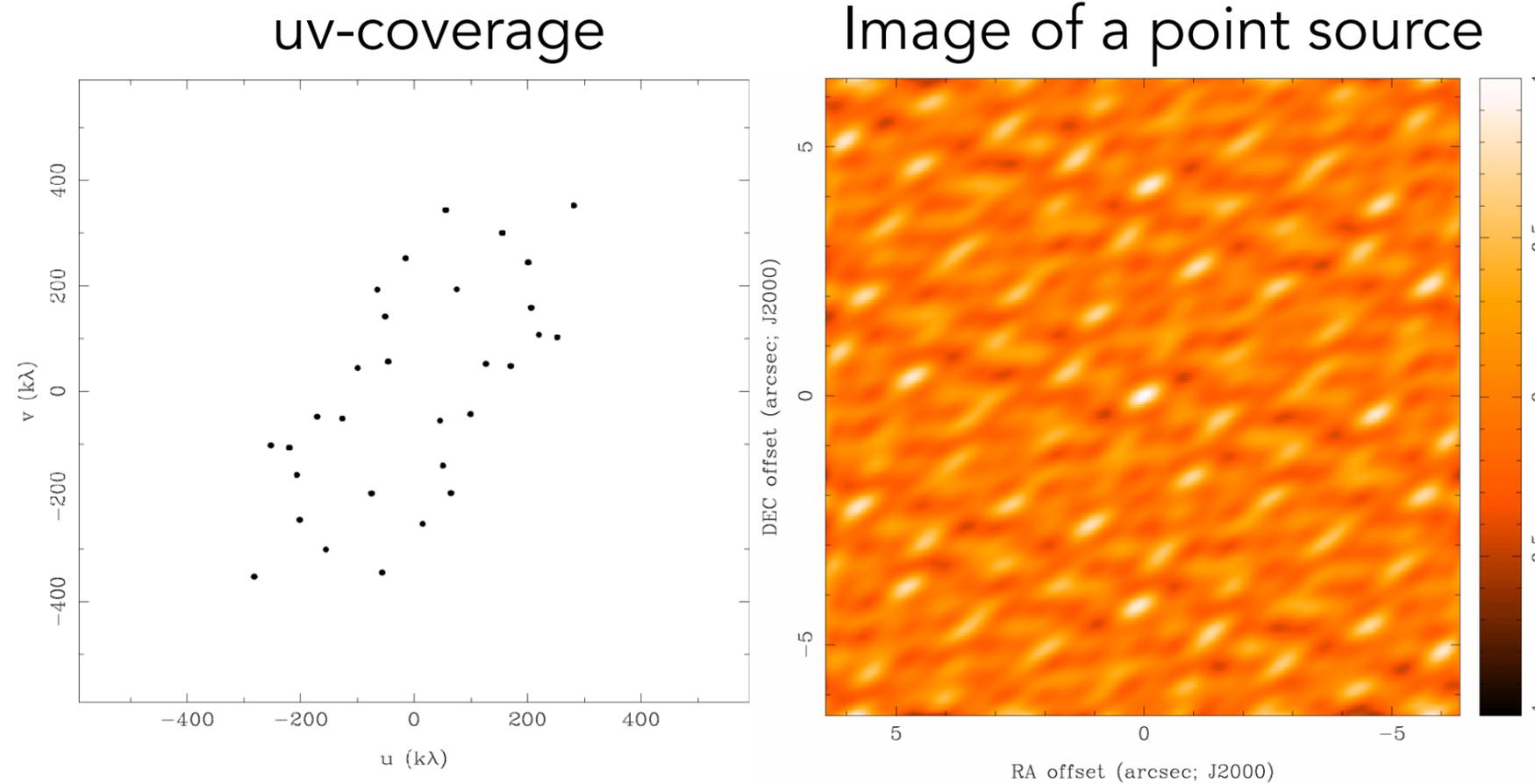


# How to maximize the sampling of $V(u,v)$ ?

Increase the number of antennas

Exploit the Earth rotation to sample different baselines

**6 antennae**

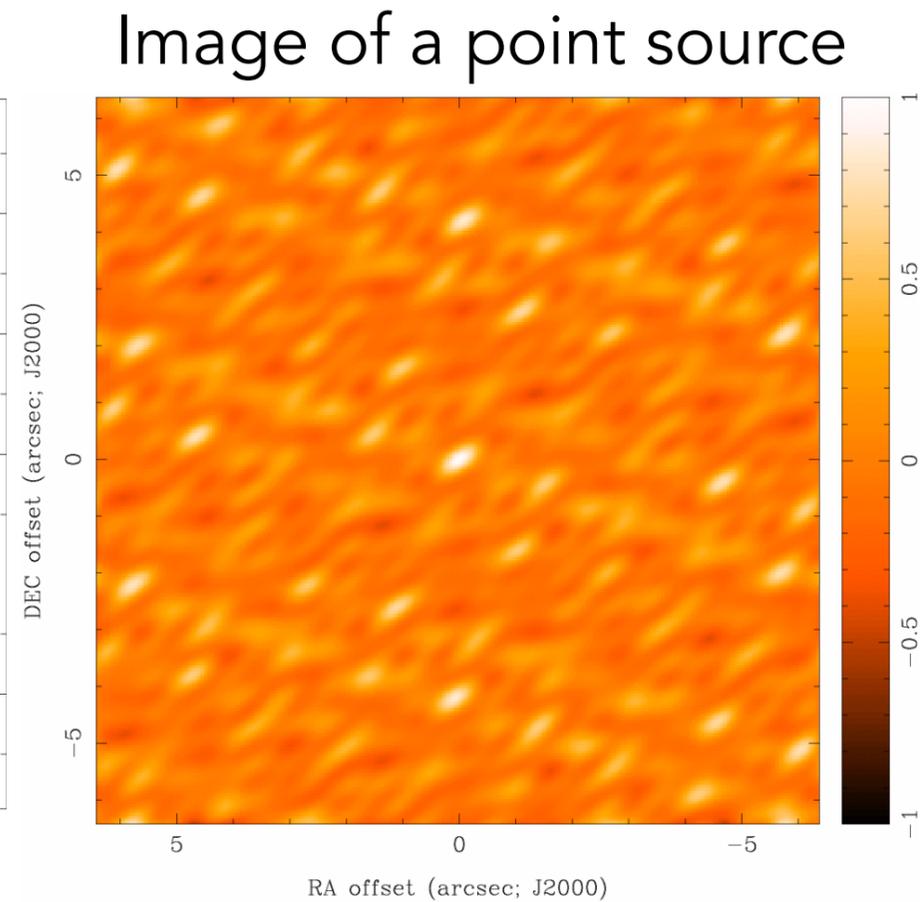
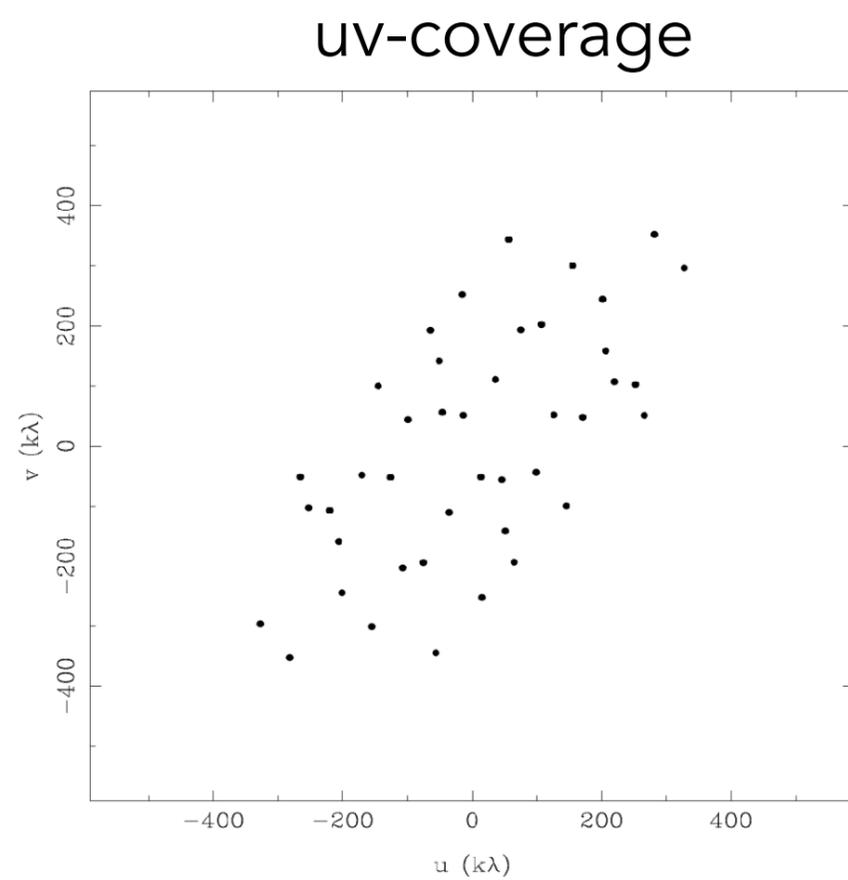


# How to maximize the sampling of $V(u,v)$ ?

Increase the number of antennas

Exploit the Earth rotation to sample different baselines

**7 antennae**

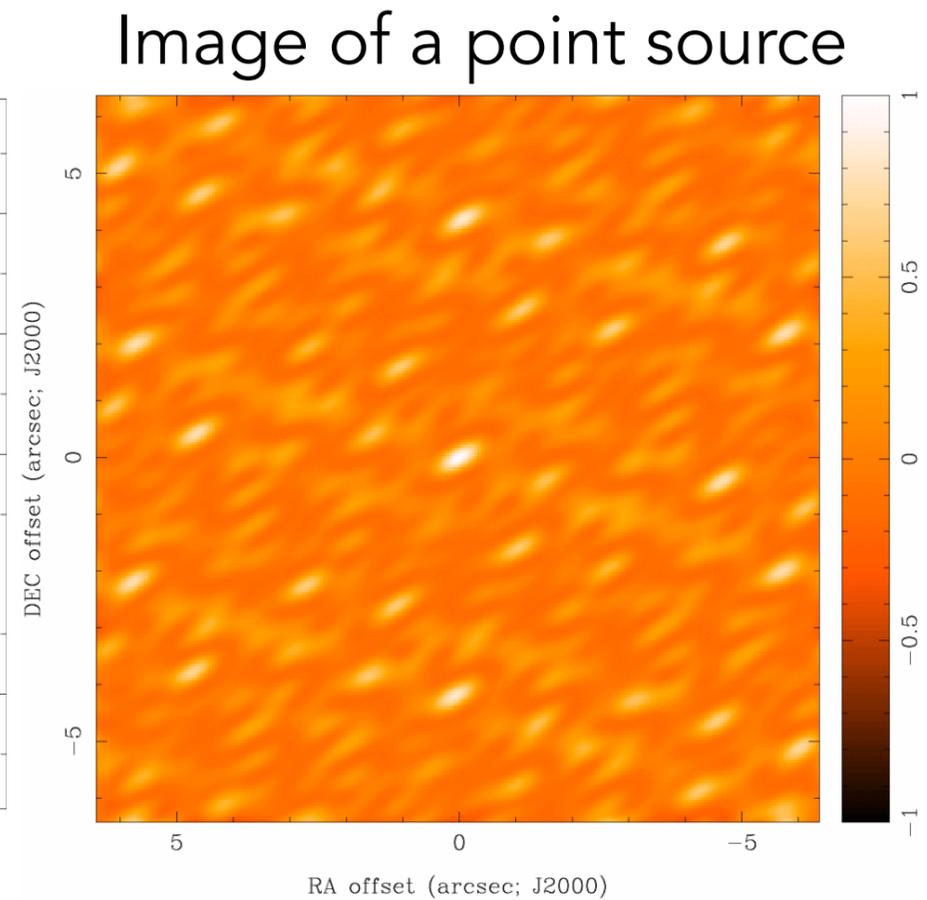
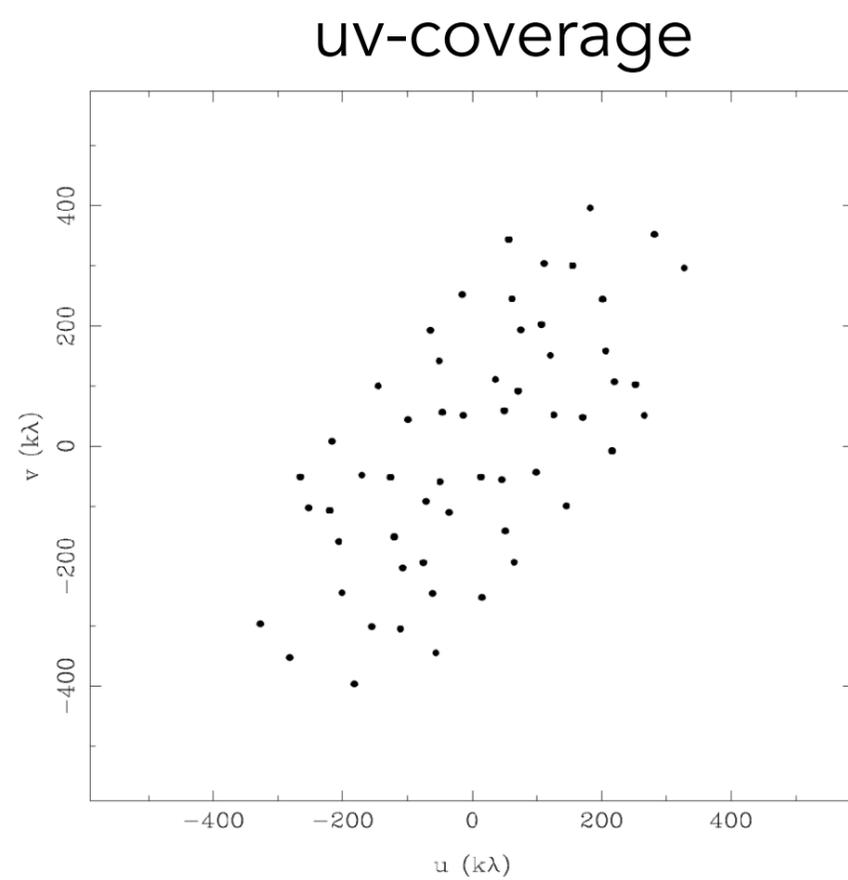


# How to maximize the sampling of $V(u,v)$ ?

Increase the number of antennas

Exploit the Earth rotation to sample different baselines

**8 antennae**



# How to maximize the sampling of $V(u,v)$ ?

Increase the number of antennas

Exploit the Earth rotation to sample different baselines

**8 antennae**  
**6 samples**

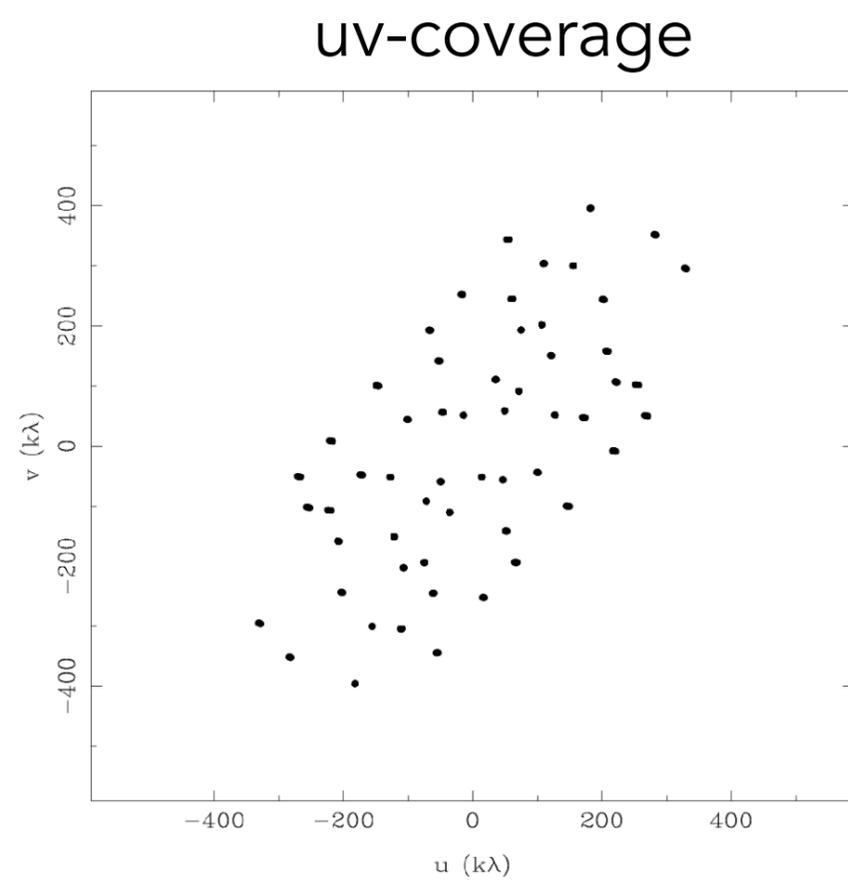
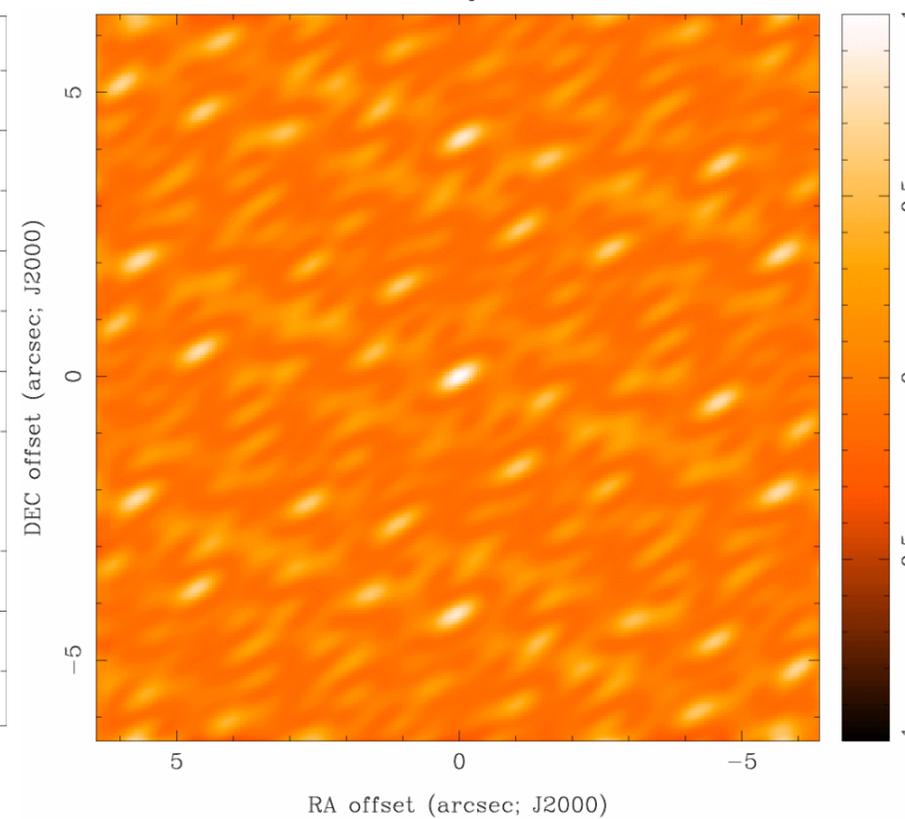


Image of a point source



# How to maximize the sampling of $V(u,v)$ ?

Increase the number of antennas

Exploit the Earth rotation to sample different baselines

**8 antennae**  
**30 samples**

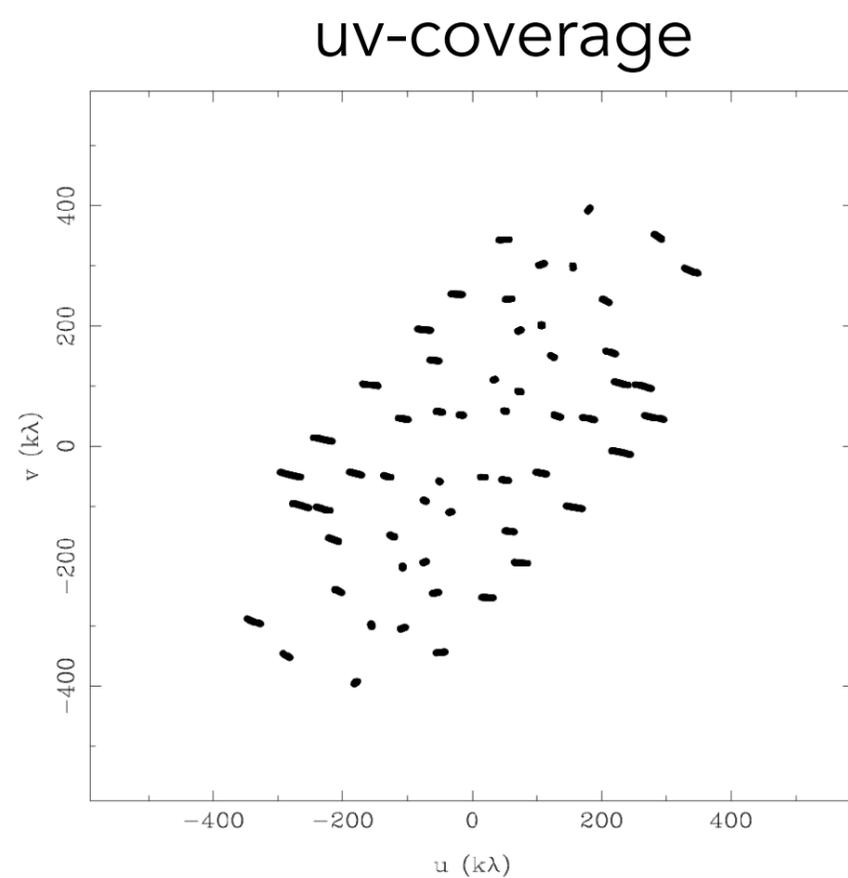
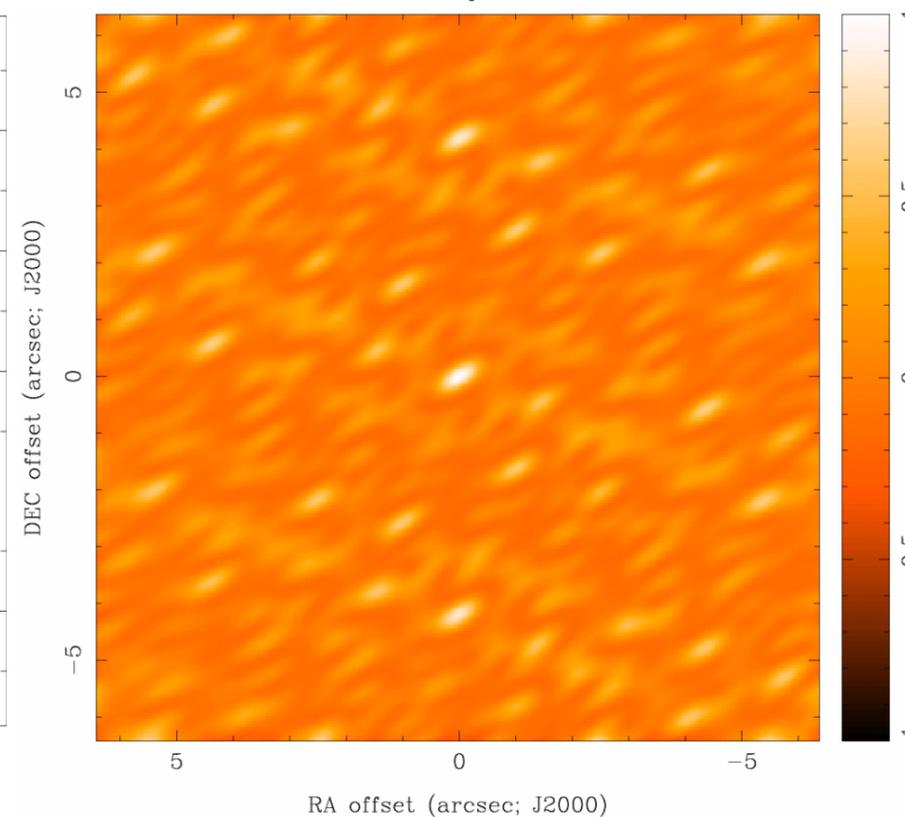


Image of a point source



# How to maximize the sampling of $V(u,v)$ ?

Increase the number of antennas

Exploit the Earth rotation to sample different baselines

**8 antennae**  
**60 samples**

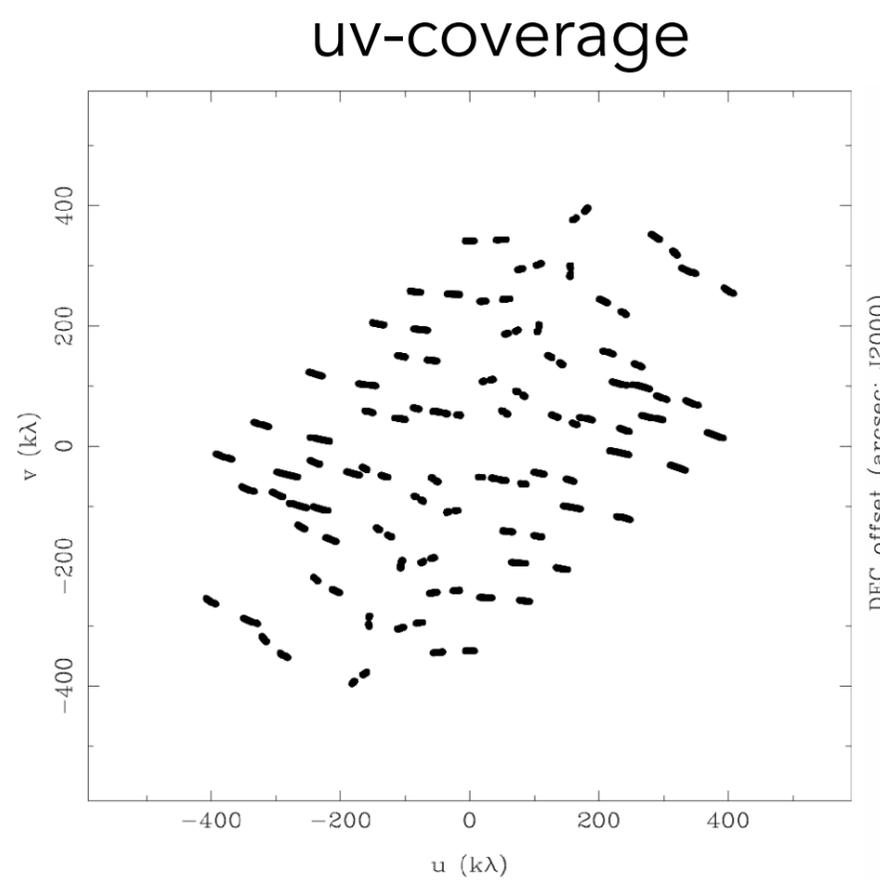
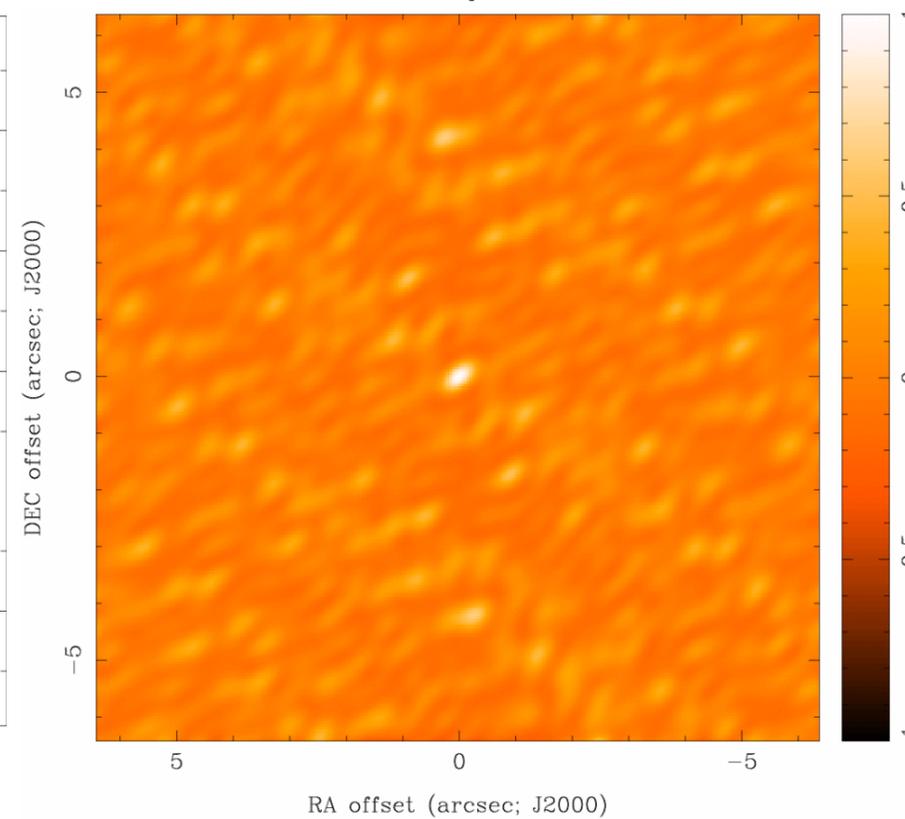


Image of a point source



# How to maximize the sampling of $V(u,v)$ ?

Increase the number of antennas

Exploit the Earth rotation to sample different baselines

**8 antennae**  
**120 samples**

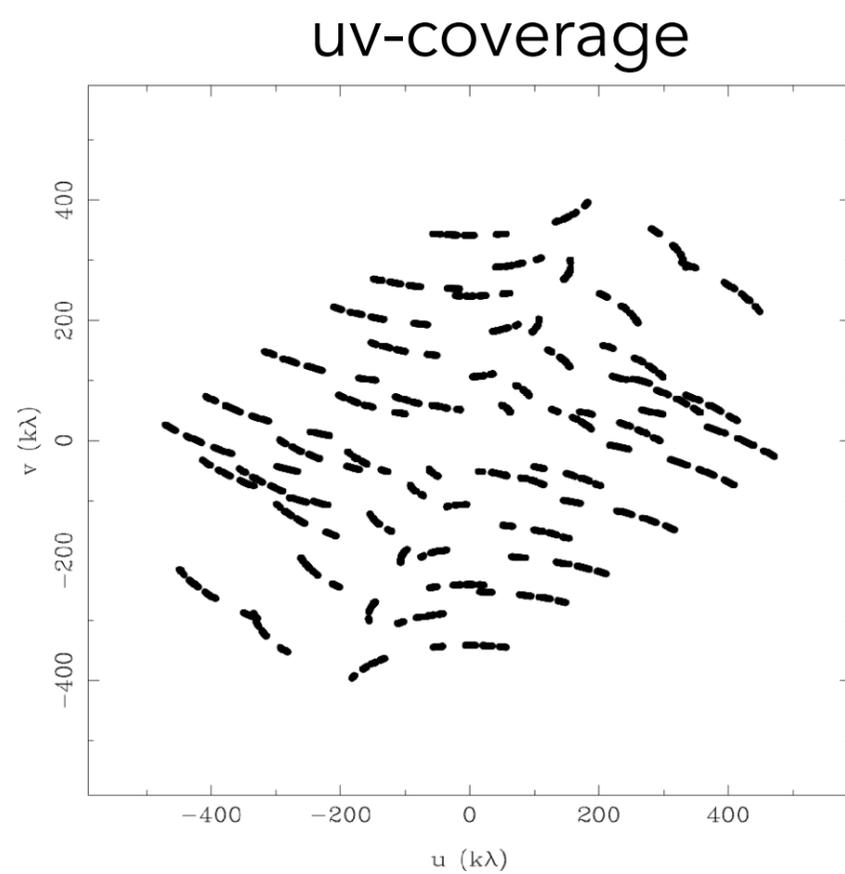
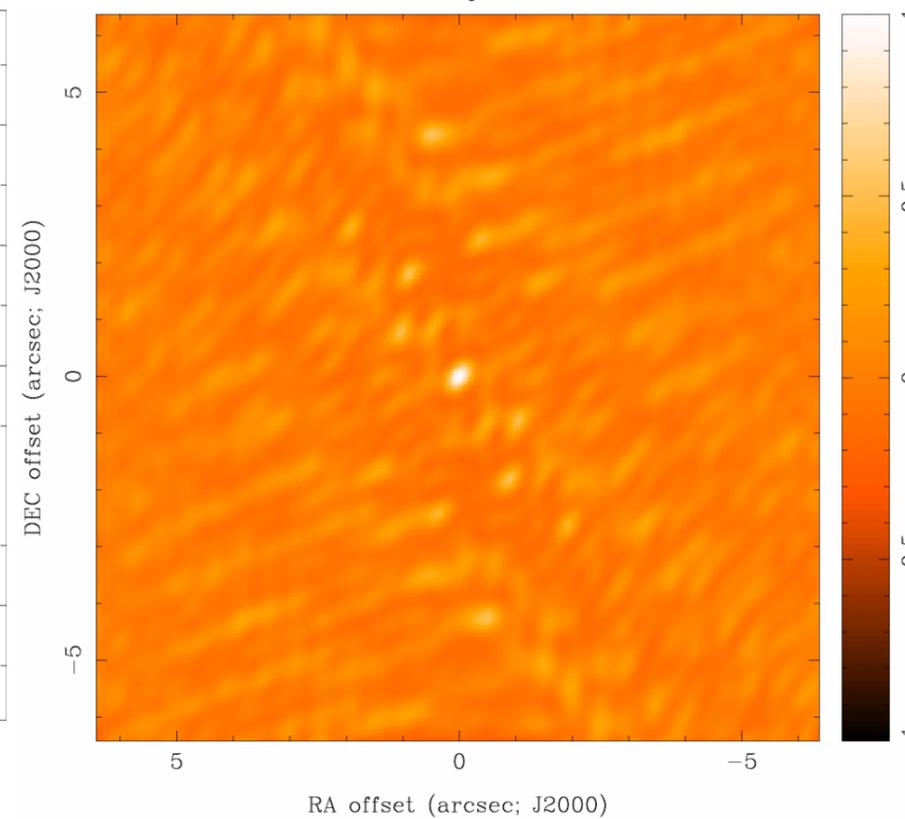


Image of a point source



# How to maximize the sampling of $V(u,v)$ ?

Increase the number of antennas

Exploit the Earth rotation to sample different baselines

**8 antennae**  
**240 samples**

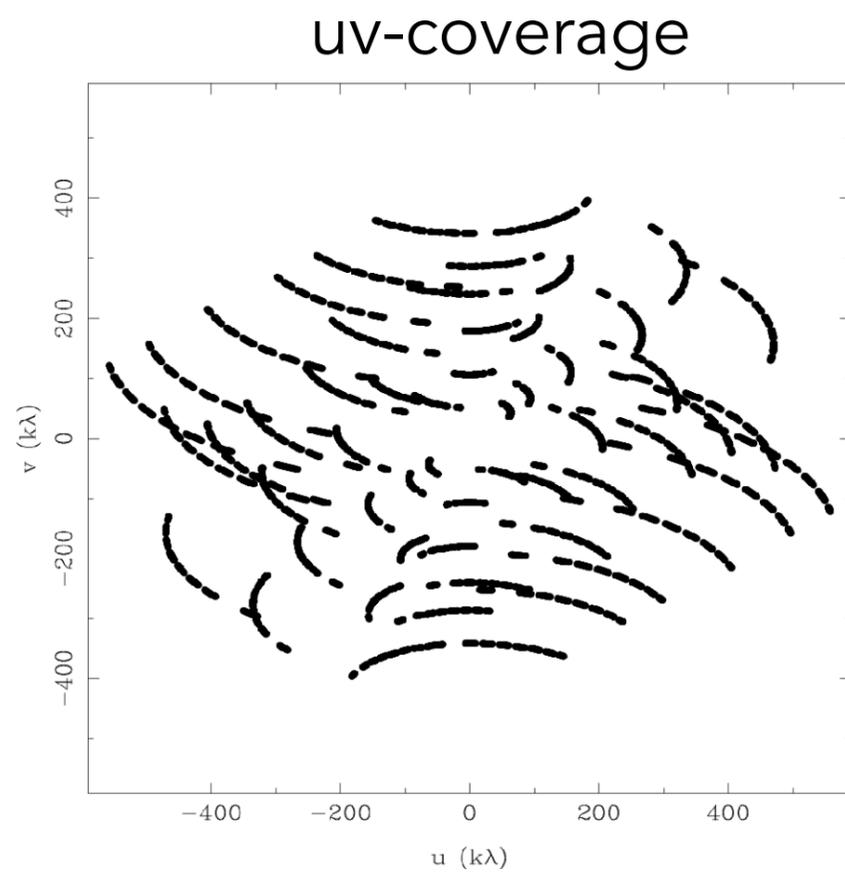
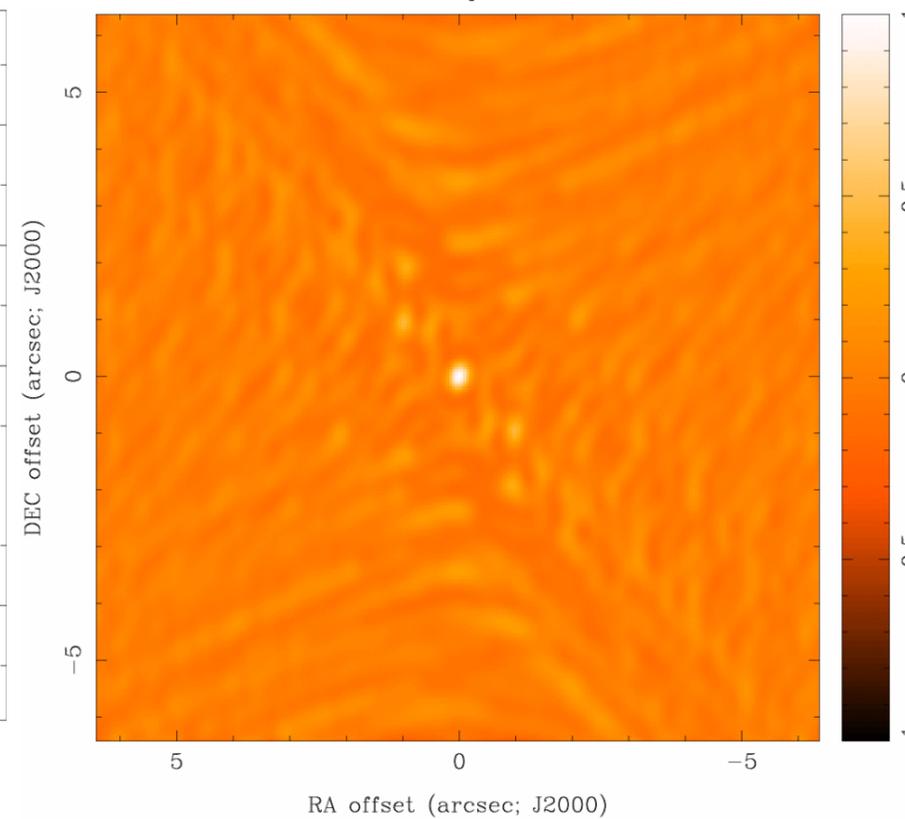


Image of a point source



# How to maximize the sampling of $V(u,v)$ ?

Increase the number of antennas

Exploit the Earth rotation to sample different baselines

**8 antennae  
480 samples**

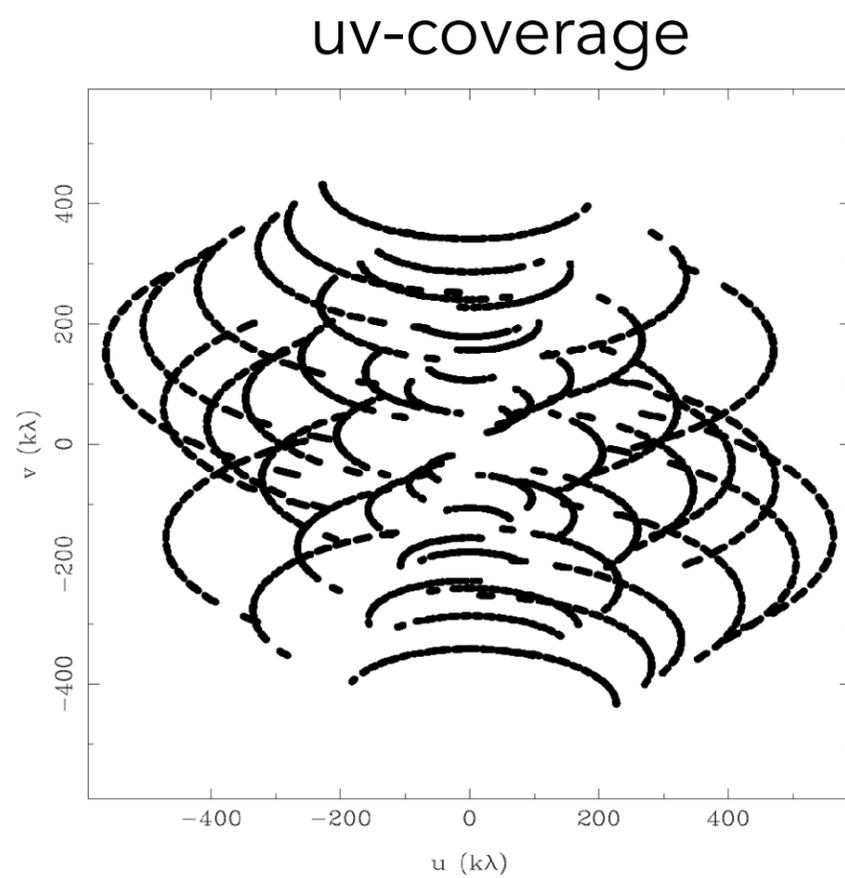
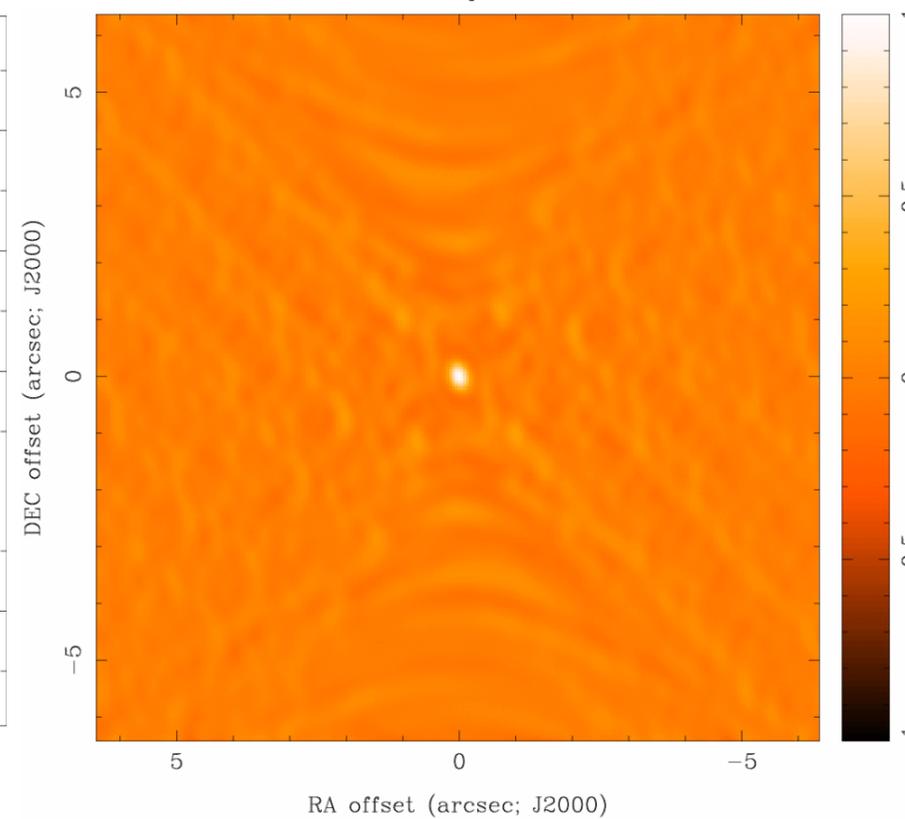
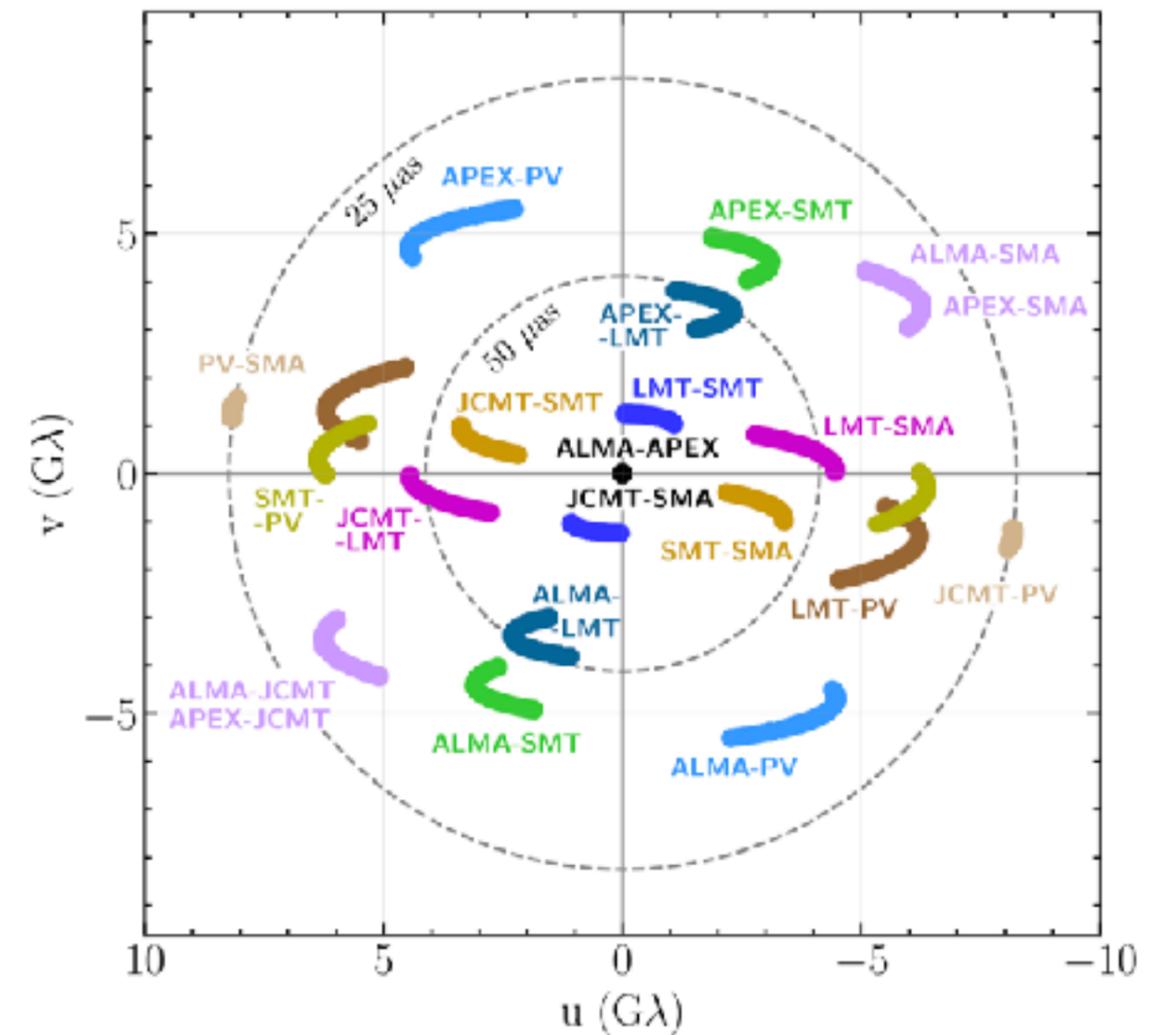
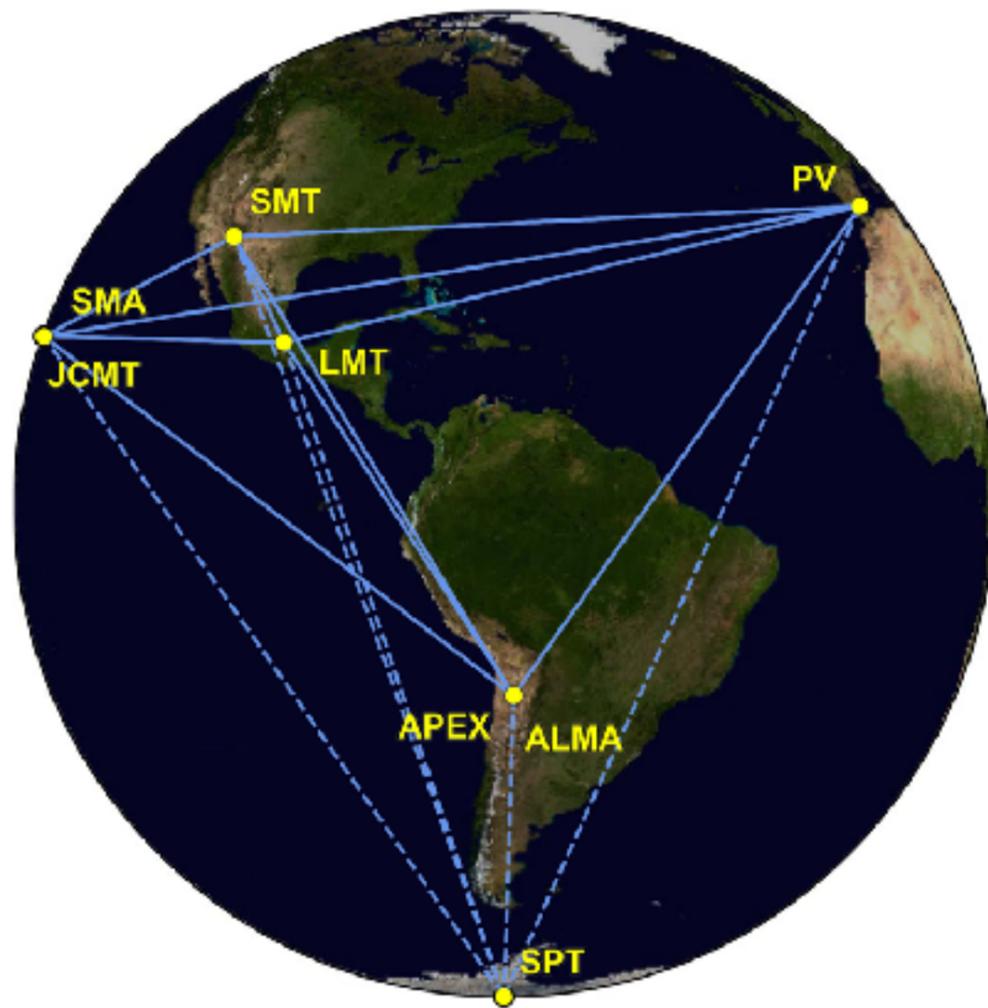


Image of a point source



# Geographical constraints can lead to peculiar uv-tracks

uv-coverage of observations of BH in M87 of the Event Horizon Telescope (EHT)



# Data calibration (examples from ALMA/VLA)

Fundamental equation of calibration

$$V_{ij}(t) = g_i(t)g_j^*(t)V^{\text{true}}(t) + \epsilon_{ij}(t)$$

$V_{ij}(t)$	visibility measured between antennas $i$ and $j$
$g_i(t)$	complex gain of antenna $i$
$V^{\text{true}}(t)$	true visibility
$\epsilon_{ij}(t)$	noise

The linear dependance between  $V_{ij}(t)$  and  $V^{\text{true}}(t)$  depends on the array design. Note that the response associated to any pair of antennas does not depend on any other pair of antennas.

At any time  $t$ , we thus have  $N(N-1)/2$  measures to obtain  $g_i(t)$  for  $N$  antennas.

# Why do we need to calibrate data?

A priori, we do not know the relation between  $V_{ij}(t)$  and  $V^{\text{true}}(t)$ . In interferometry, calibrators are observed every hour, and the calibrations are not shared with other observations (differently from optical/IR telescopes) for the following reasons:

The gain functions depend on the troposphere and ionosphere, and how they affect the wave front. But these have a spatial dependance.

- The ionosphere can offset phase by  $1^\circ/\text{s}$  on baselines  $>10$  km
- Electronics can change with time
- Other observations may not be optimized for another observation

# Calibrators

The best way to solve the calibration equation is to use calibrators that are very well characterised and stable: Best option is point sources that are bright in cm-mm. If they are point sources, the phase will be zero (assuming that the phase center corresponds to the location of the calibrator)

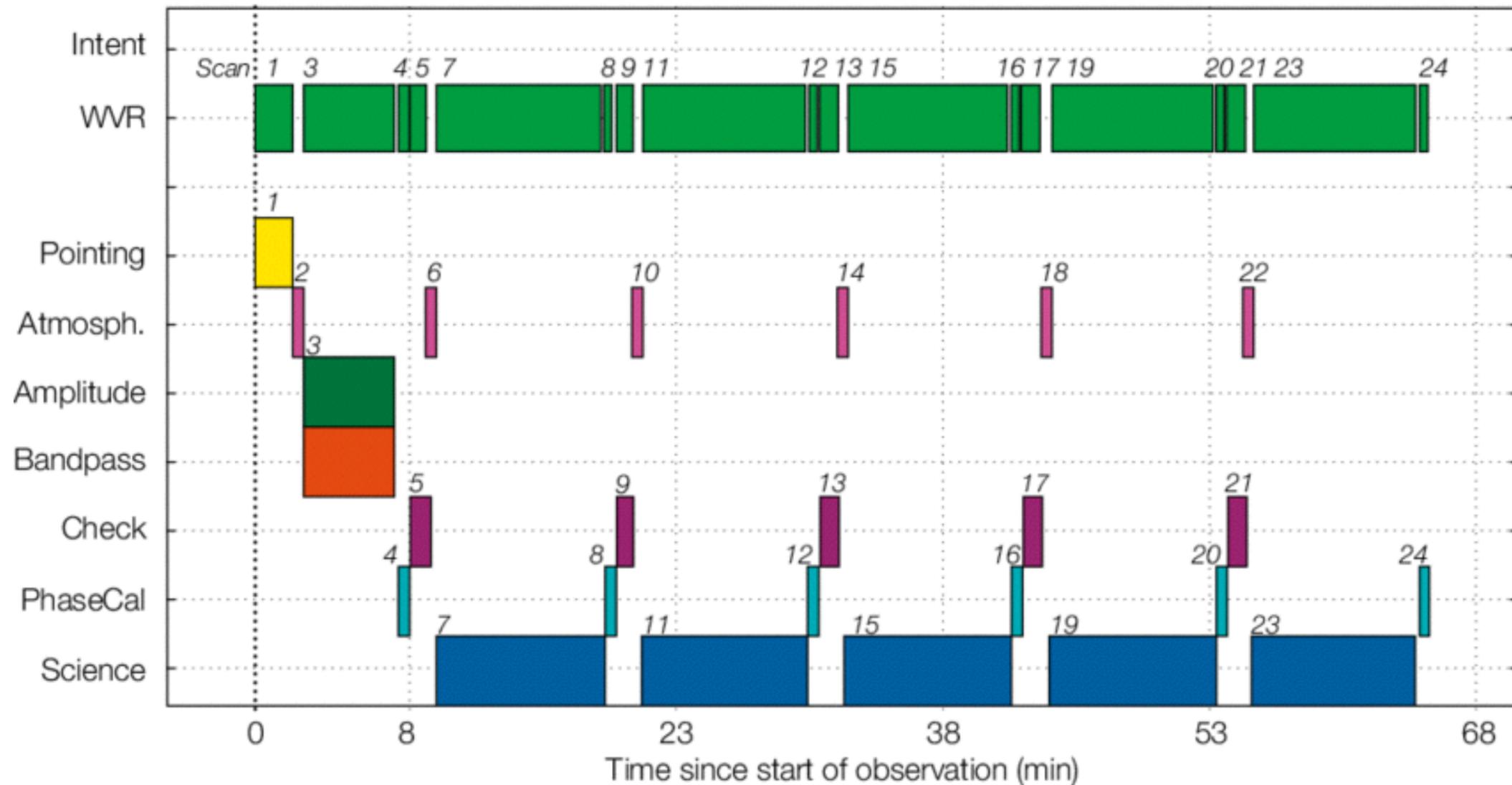
$$V_{ij}(t) = g_i(t)g_j^*(t)V^{\text{true}}(t) + \epsilon_{ij}(t)$$

The gain functions are computed on the calibrators, and are then applied to the scientific observations (cross-calibration)

# Example from ALMA data

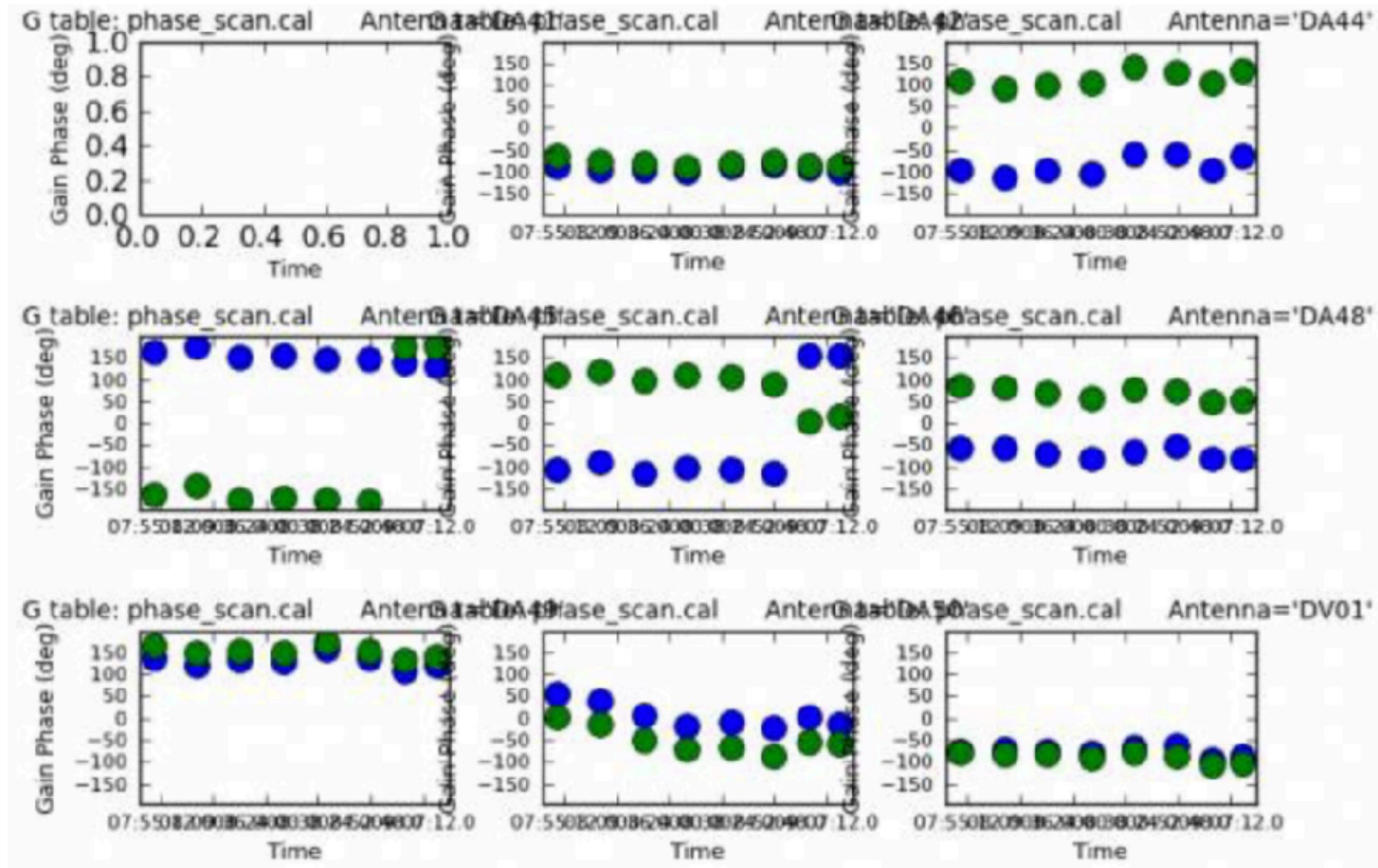
3 fundamental calibrations for every observation:

- Flux calibration
- Passband calibration (spectral dependance)
- Phase calibration



# Example from ALMA data

Gain functions computed using the phase-calibrator (two colors show two different polarizations).

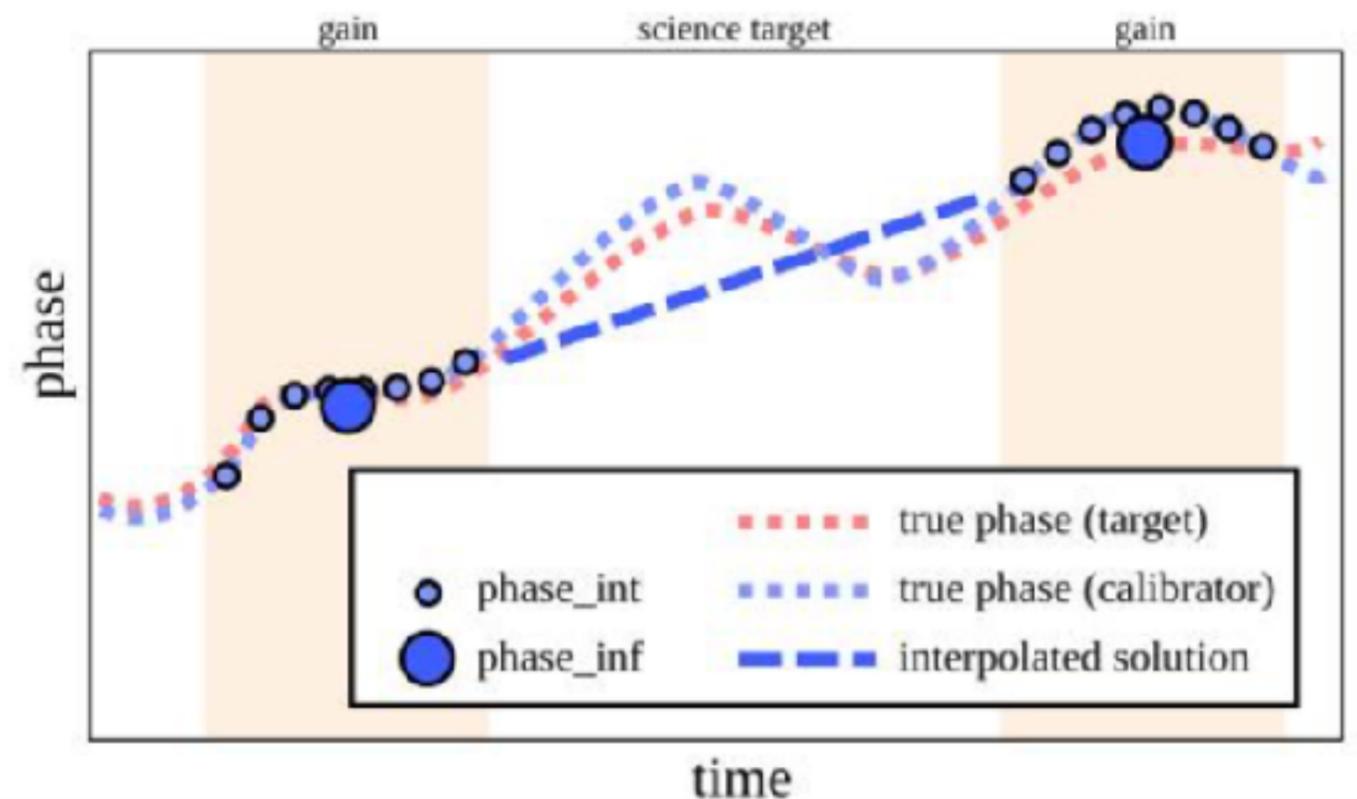
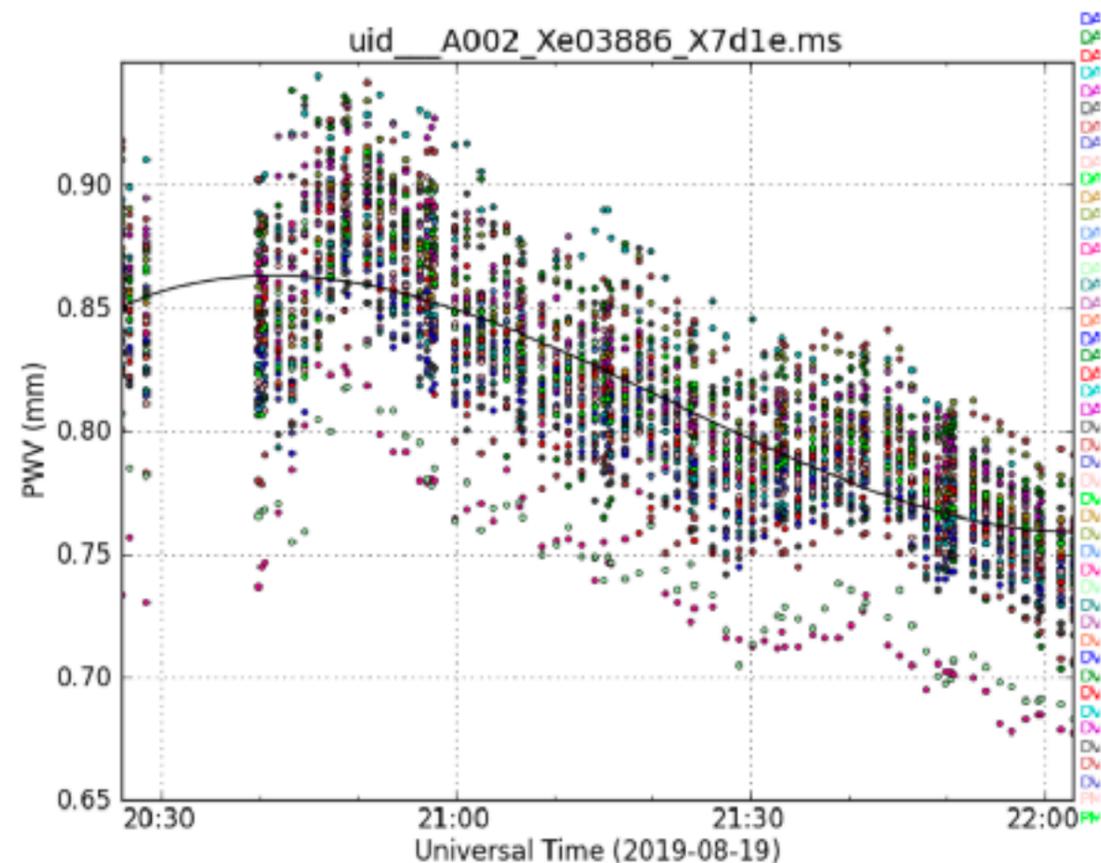


# Self-calibration

If the astrophysical source is very bright, it is possible to solve the calibration equation using the source itself, after having applied the cross-calibration.

This practise has the following advantages:

- The gain functions can be computed more frequently (both phase and amplitude)
- The gain functions are computed in the same of the source (pointing changes with calibrators)

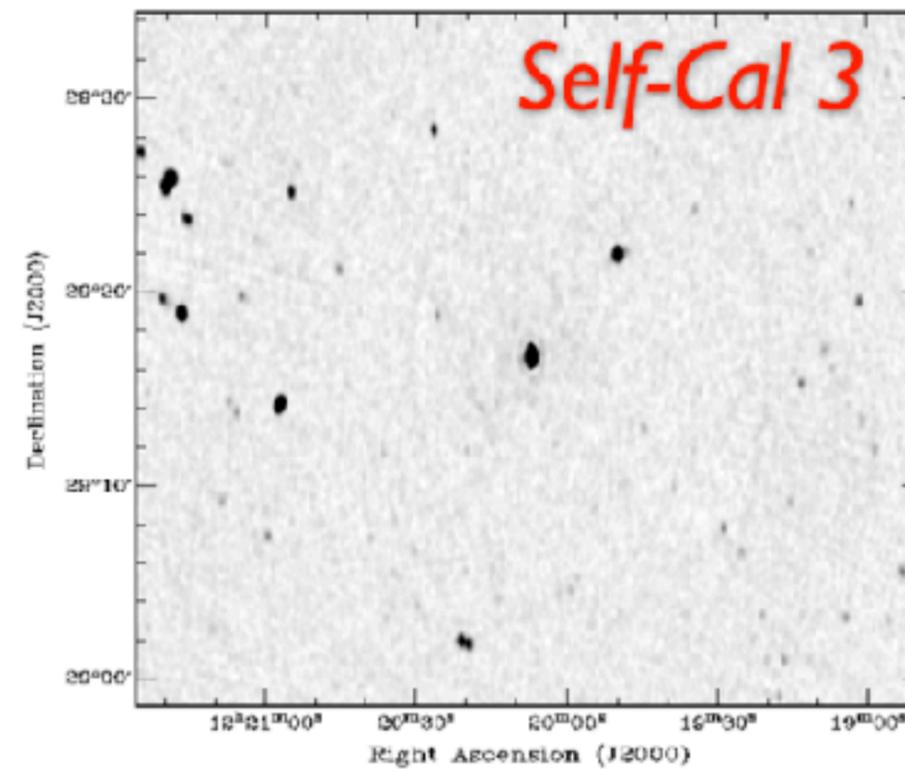
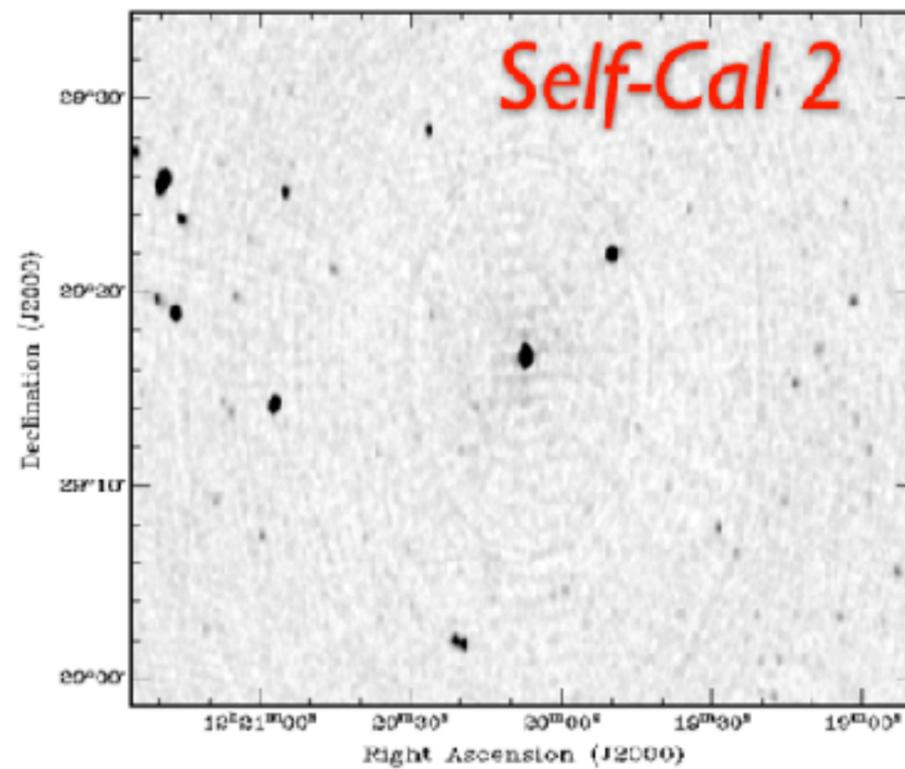
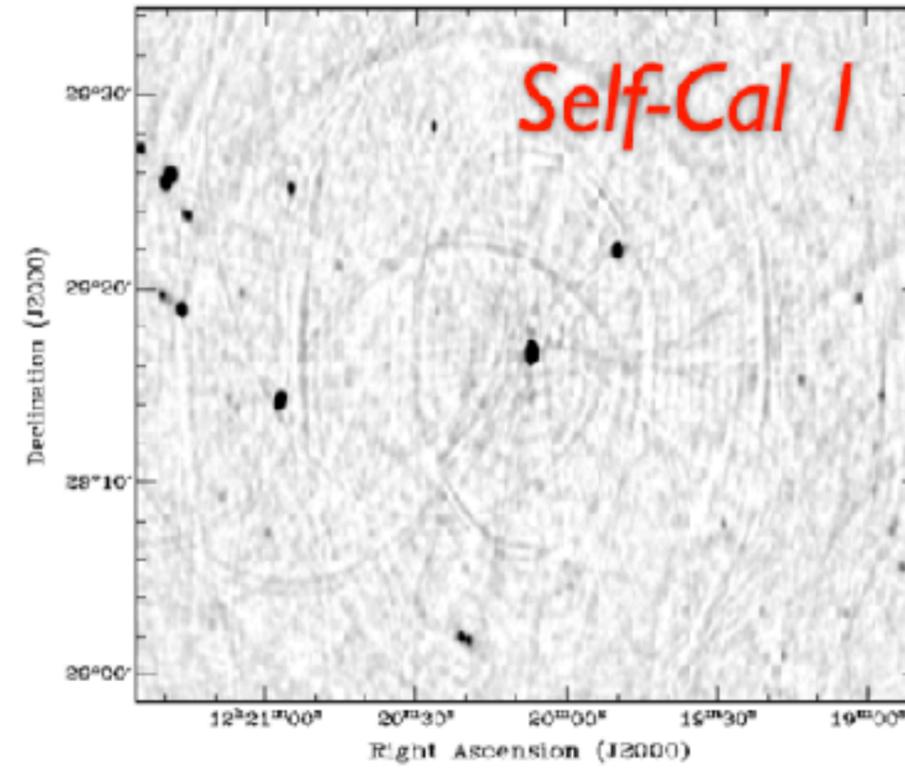
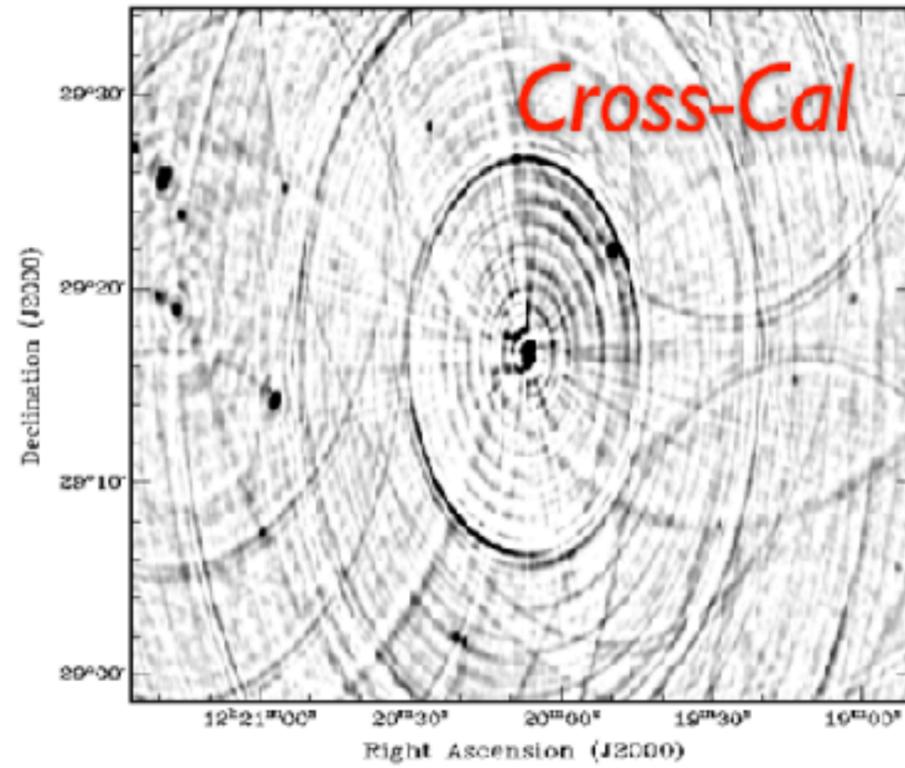


# Self-calibration

It's an iterative process:

1. I compute the image after having applied the cross-calibrations (we see soon how to make an image).
2. I use the Fourier transform of this image as  $V^{\text{true}}$  to compute the gain functions on a shorter time interval than the former one.
3. I re-compute the image and check that the quality has improved
4. I go back to point 2) and I keep going as long as my image quality improves (in this school we will not go into details of what 'image quality' means in interferometry, but for a first approach just use the snr.)

# Examples of self-calibration



# Examples of self-calibration

Cygnus A

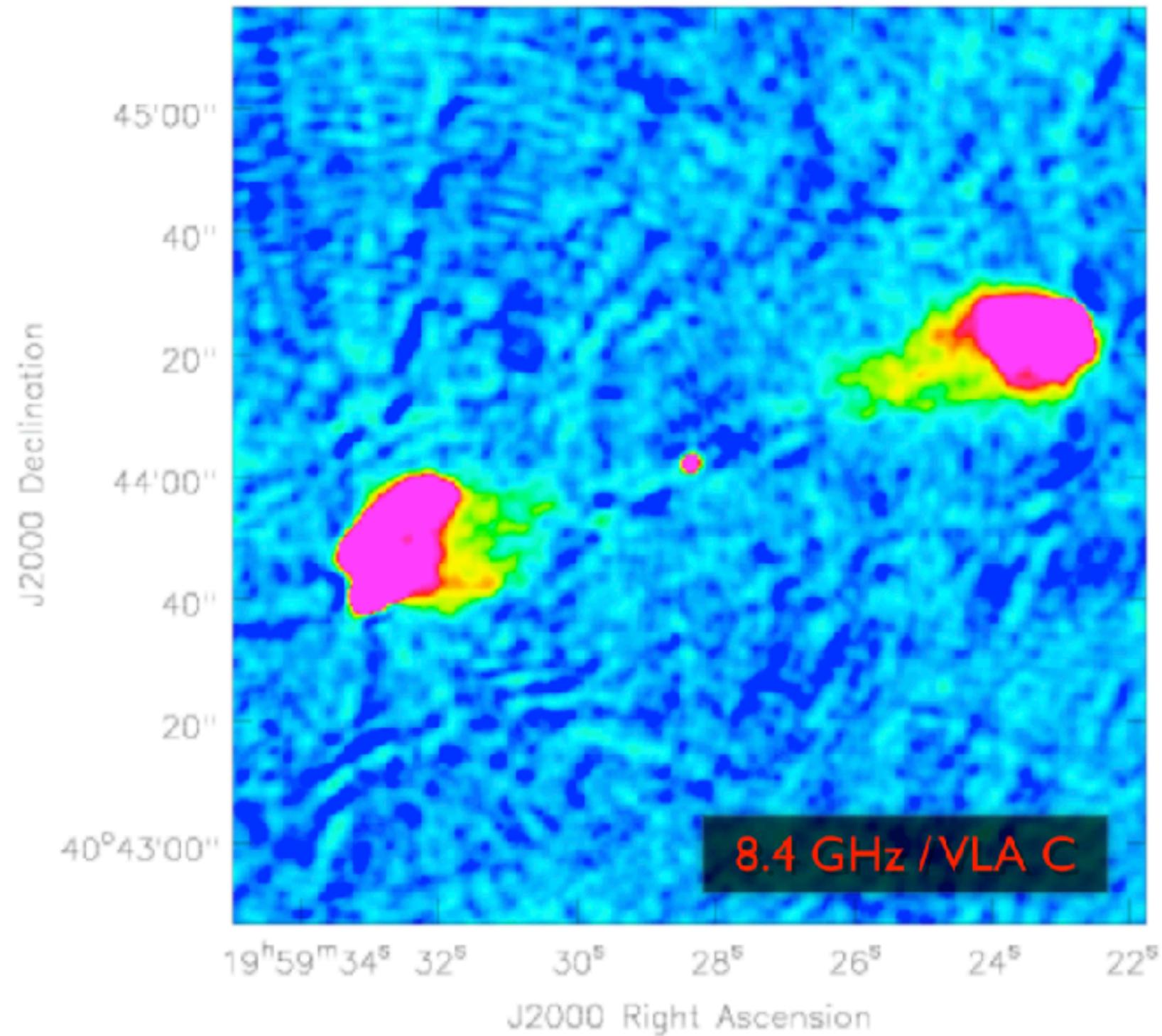
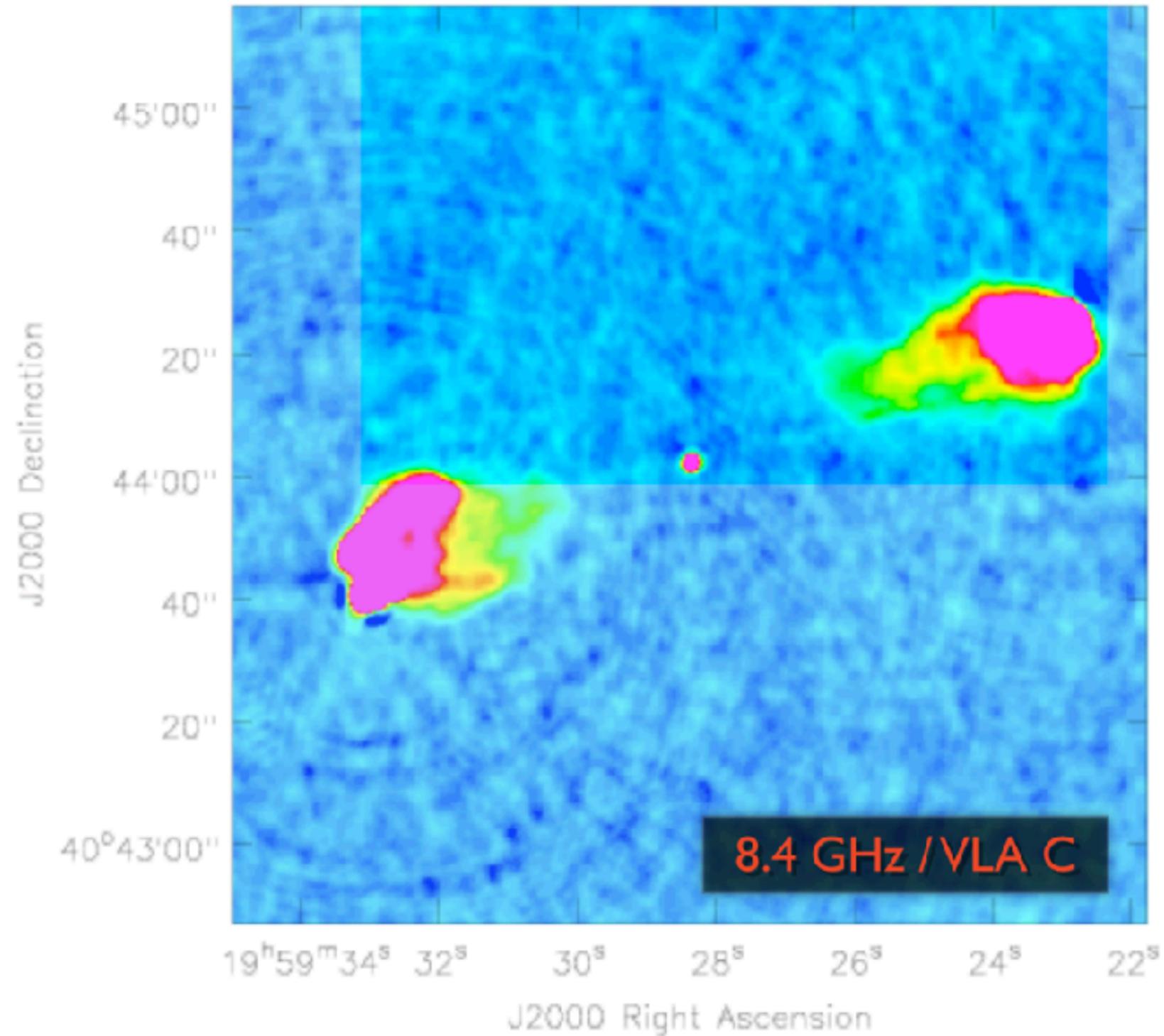


Image without self-calibration

# Examples of self-calibration

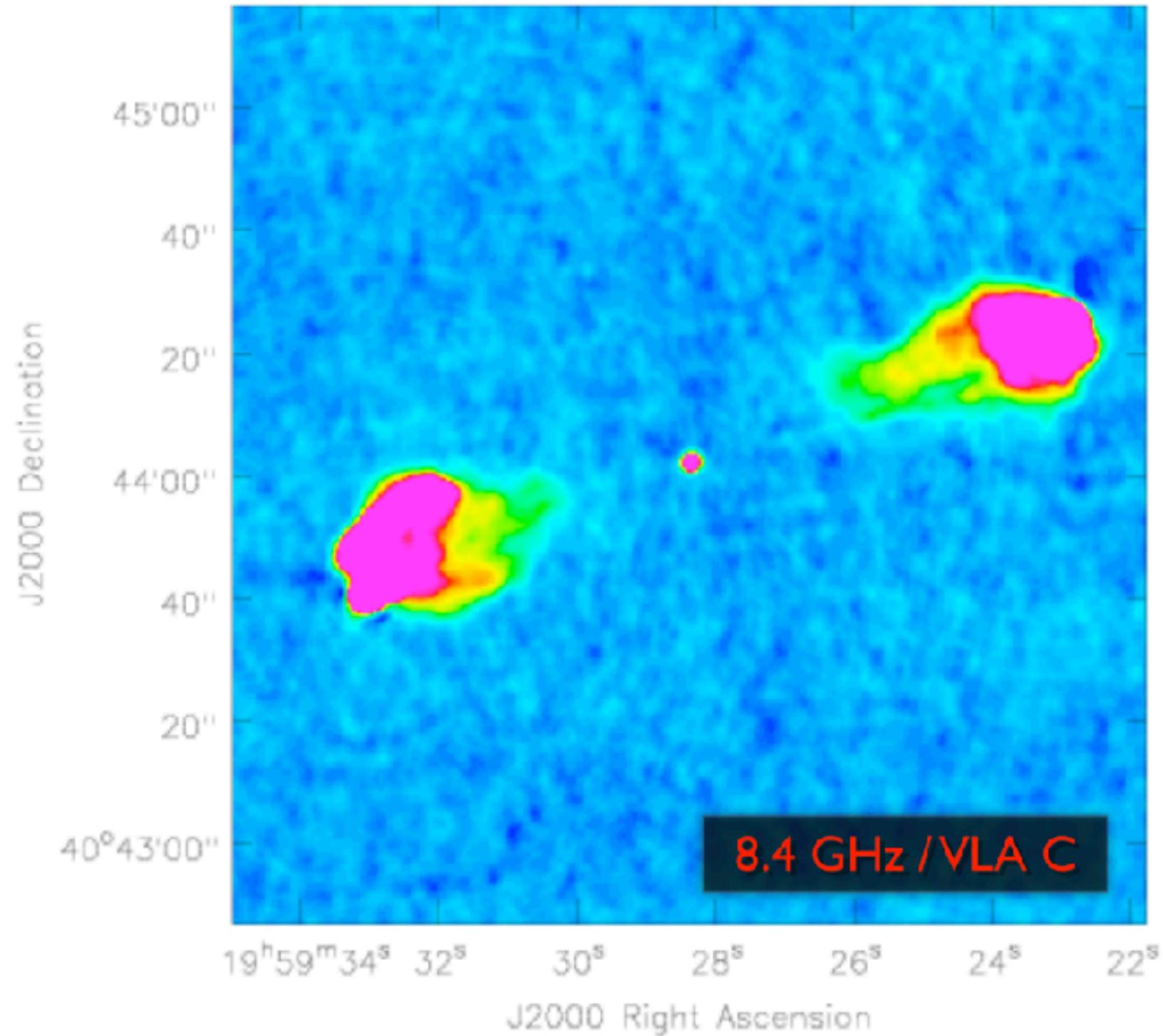
Cygnus A



After 1 phase self-cal

# Examples of self-calibration

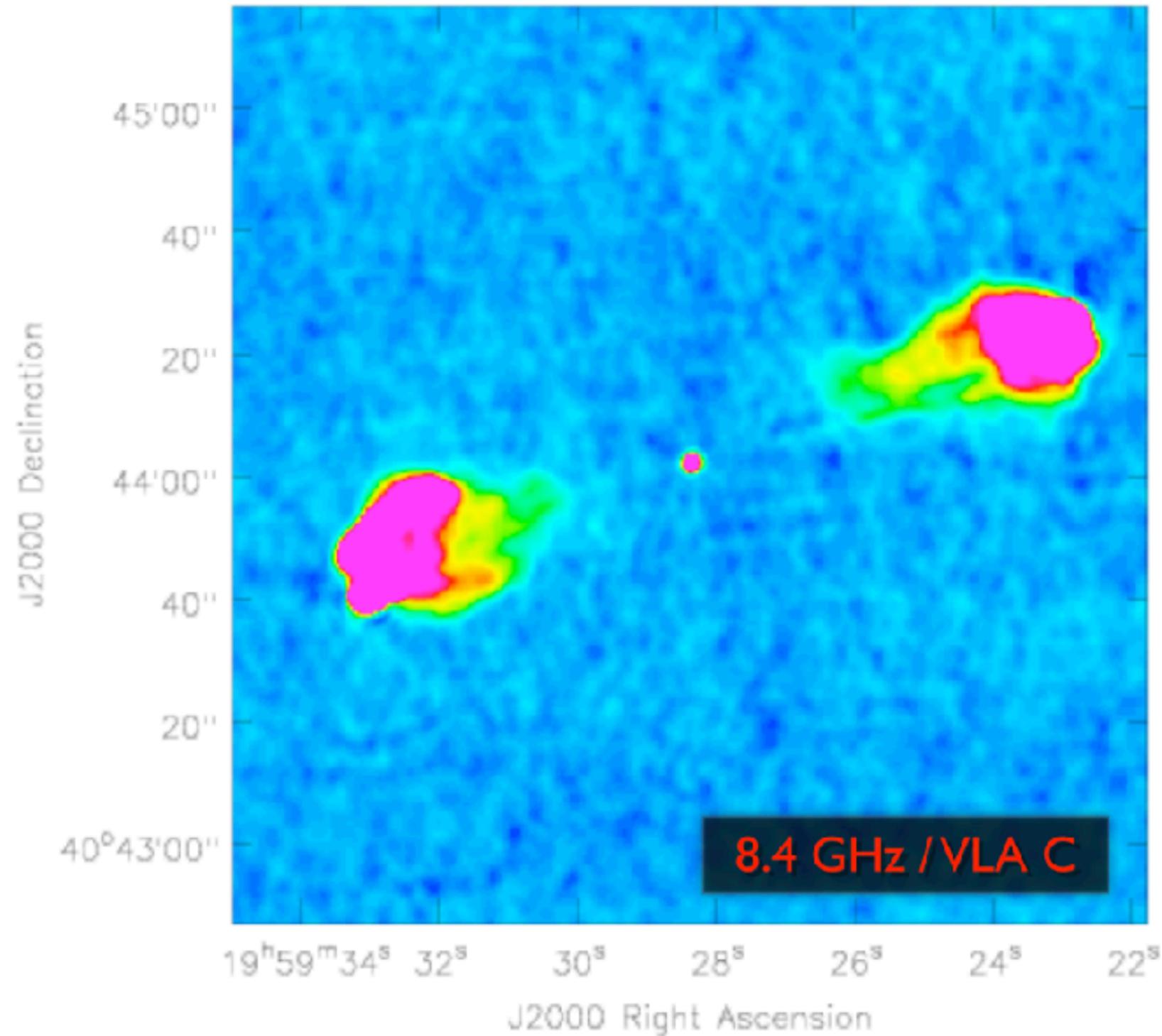
Cygnus A



After 1 phase and amplitude self-cal

# Examples of self-calibration

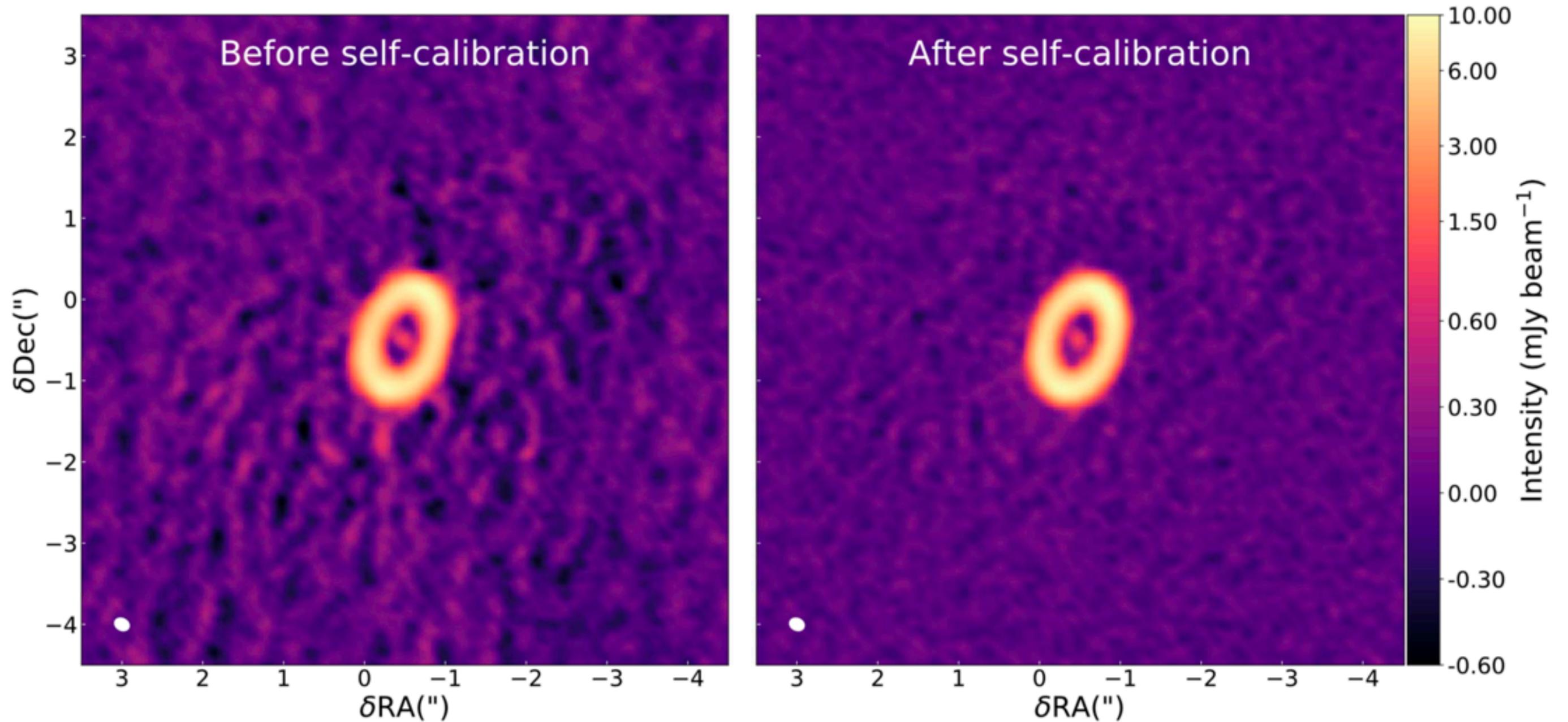
Cygnus A



After 4 rounds of phase and amplitude self-cal

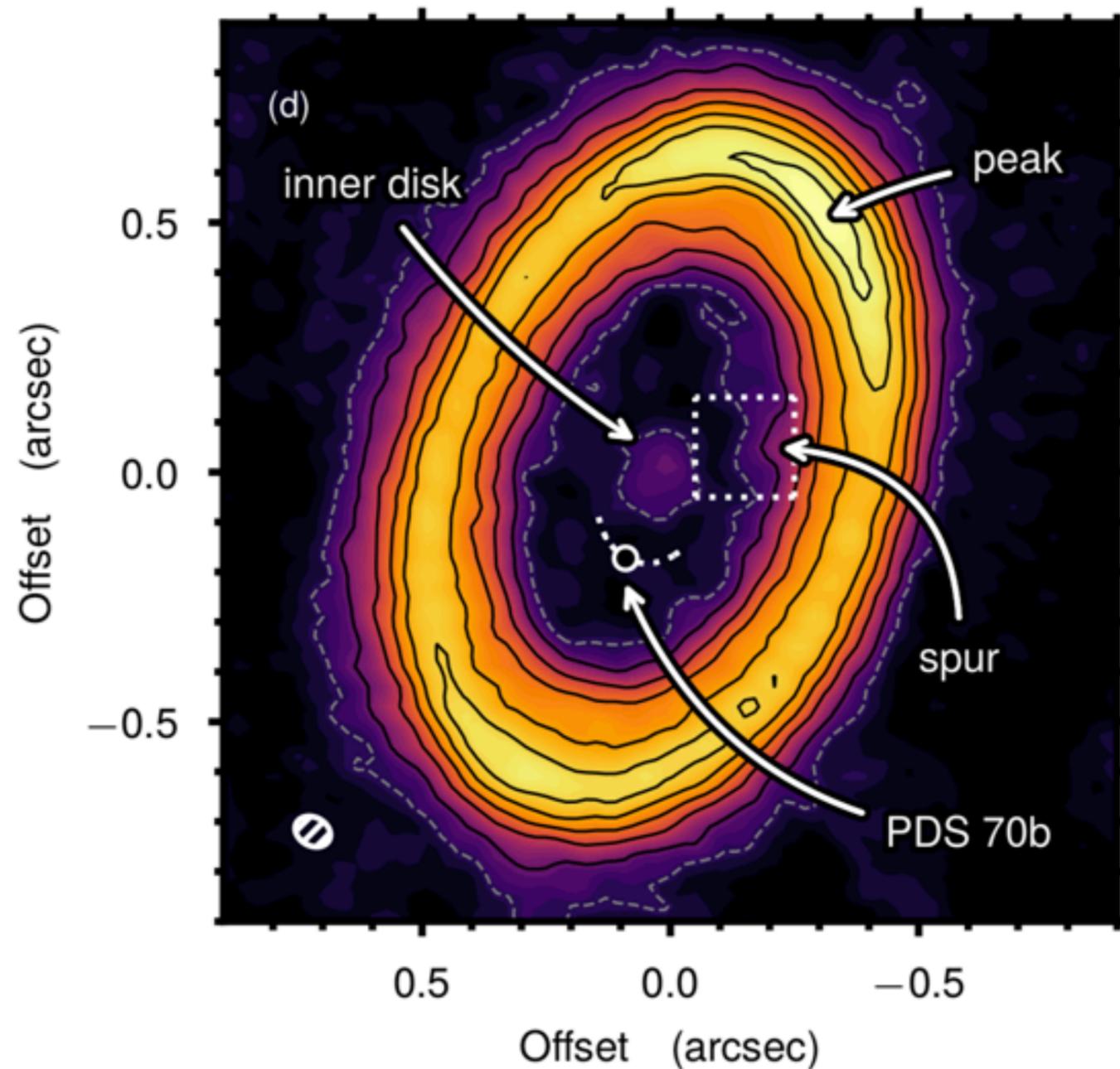
# Examples of self-calibration

PDS 70: discovery of first circumplanetary disk

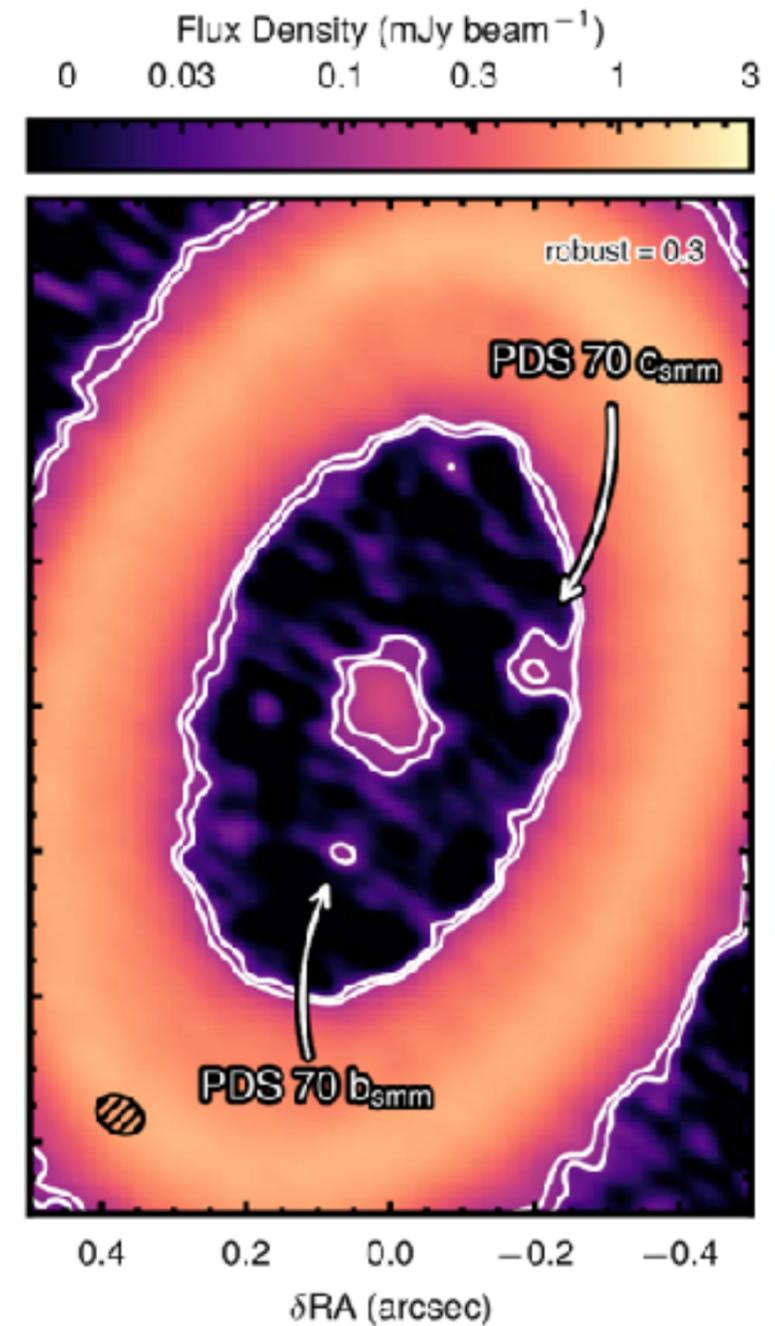


# Examples of self-calibration

PDS 70: discovery of first circumplanetary disk



First attempt of self-cal (Keppler+2019)



Improved self-cal (Isella+2019)

# Examples of self-calibration

PDS 70: discovery of first circumplanetary disk



Higher resolution data confirmed the presence of a candidate CPD (Benisty+2021)